



**NUS**  
National University  
of Singapore

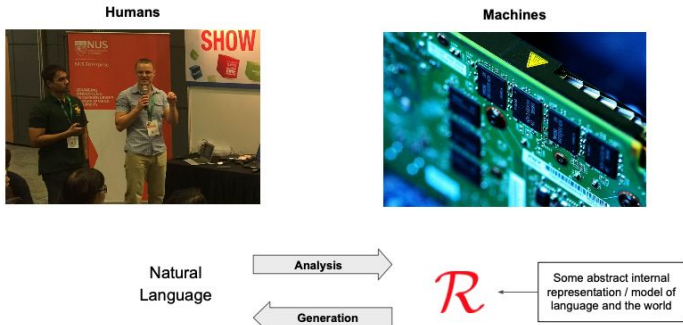
| **Computing**

# **CS4248: Natural Language Processing**

## **Lecture 2 — Strings & Words**

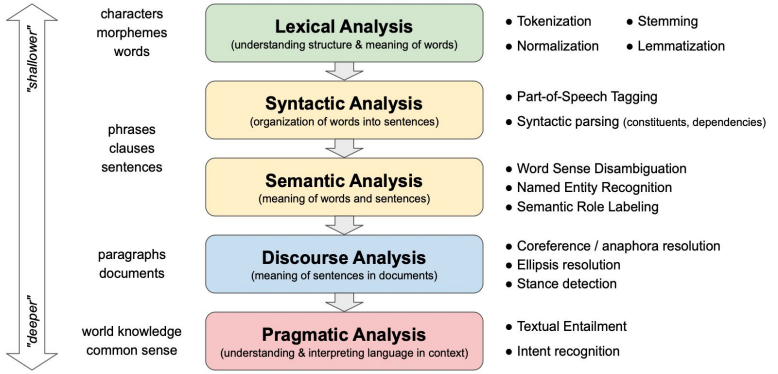
# Recap of Week 01

## Communication with Machines



Source: Wiki Common (CC BY-SA 4.0); [gdu](#)

## NLP in One Slide



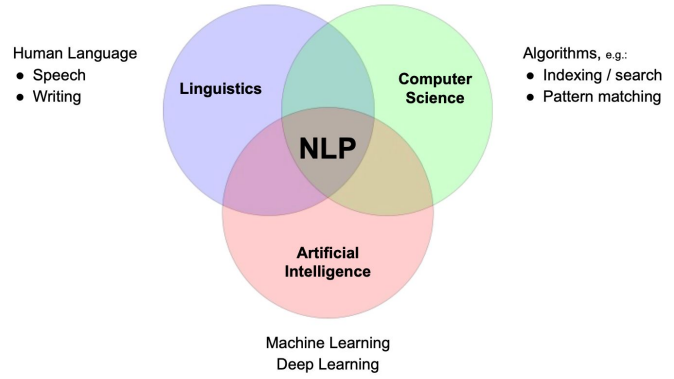
## DYI Winograd Schema

(5 minutes)

**Find and post your own examples for Winograd Schema(s)**

Explain what is ambiguous about it.  
Go wild! Find good interesting ones.  
Give kudos and upvote your peers!

## What is NLP? — The Bigger Picture



# Outline

- **Regular Expressions**
  - **Basic Concepts**
  - Relationship to FSA
  - Error Types
- **Corpus Preprocessing**
  - Tokenization
  - Normalization
  - Stemming / Lemmatization
  - Segmentation
- **Word error handling**
  - Spelling Errors
  - Minimum Edit Distance
  - Noisy Channel Model

# Regular Expressions

- Regular Expression — Definition

- Search pattern used to match character combinations in a string
- Pattern = sequence of characters

- Common applications

- Parse text documents to find specific character patterns
- Validate text to ensure it matches predefined patterns
- Extract, edit, replace, delete substrings matching a pattern

- Two basic search approaches

- Default: match only first occurrence of pattern
- Global search: match all occurrences of pattern (assumed in most following examples)

**Example: password validation**

- \* Must have a minimum of 8 characters
- \* Must not contain username
- \* Must include at least 1 uppercase
- \* Must include at least 1 lowercase
- \* Must include at least 1 digit or 1 special character:  
~ ! @ # \$ % ^ & \* \_ - + = ` | \ ( ) { } [ ] ; : ' < > , . ? /

# Basic Patterns

- Fixed patterns

`floor` → *My block has 15 floors, and I live on floor 5.*

`5` → *My block has 15 floors, and I live on floor 5.*

`blocks` → *My block has 15 floors, and I live on floor 5.*

- Special characters (metacharacters)

| Character | Explanation                                                                        |
|-----------|------------------------------------------------------------------------------------|
| .         | matches any character except line breaks                                           |
| ^         | match the start of a string                                                        |
| \$        | match the end of a string                                                          |
|           | matches RegEx either before or after the symbol (e.g., <code>floor floors</code> ) |
| \b        | matches boundary between word and non-word                                         |

# Character Classes

- Character class

- Defines set of valid characters
- Enclosed using "[...]"
- Can be negated: "[^...]"

`[0-9][0-9]` → *My block has 15 floors, and I live on floor 5.*

(match all sequences of 2 digits)

`[.,;:]` → *My block has 15 floors, and I live on floor 5.*

(match all sequences of length 1 that are either a period, comma, etc.)

`[^a-z]` → *My block has 15 floors, and I live on floor 5.*

(match all sequences of length 1 that are not a lowercase letter)

# Predefined Character Classes

- Common character classes with their own shorthand notation (i.e., metacharacters)

| Class     | Alternative   | Explanation                          |
|-----------|---------------|--------------------------------------|
| <b>\d</b> | [0-9]         | matches any digit                    |
| <b>\D</b> | [^0-9]        | matches any non-digit                |
| <b>\s</b> | [ \n\r\t\f]   | matches any whitespace character     |
| <b>\S</b> | [^ \n\r\t\f]  | matches any non-whitespace character |
| <b>\w</b> | [a-zA-Z0-9_]  | matches any word character           |
| <b>\W</b> | [^a-zA-Z0-9_] | matches any non-word character       |

# Repetition Patterns

- Very common: patterns with flexible lengths, e.g.:
  - All numbers with more than 2 digits
  - All words with less than 5 characters
- Repetition patterns — metacharacters

| Pattern      | Explanation                                                                                   |
|--------------|-----------------------------------------------------------------------------------------------|
| <b>+</b>     | 1 or more occurrences                                                                         |
| <b>*</b>     | 0 or more occurrences                                                                         |
| <b>?</b>     | 0 or 1 occurrences                                                                            |
| <b>{n}</b>   | exactly <i>n</i> occurrences                                                                  |
| <b>{l,u}</b> | between <i>l</i> and <i>u</i> occurrences; can be unbounded: { <i>l</i> , } or { , <i>u</i> } |

# Repetition Patterns — Examples

`\d{2,}` → *My block has 15 floors, and I live on floor 5.*  
(match all numbers with 2 or more digits)

`\d+` → *My block has 15 floors, and I live on floor 5.*  
(match all numbers with 1 or more digits)

`\b\w{2,4}\b` → *My block has 15 floors, and I live on floor 5.*  
(match words with 2 to 4 characters)

`\b[Ff]loor[s]? \b` → *My block has 15 floors, and I live on floor 5.*  
(match occurrences of "floor", either capitalized or not, either in singular or plural)

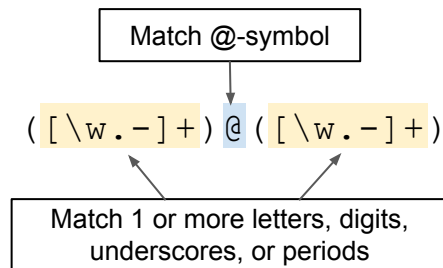
# Groups

**Quick quiz:** In which case(s) would the RegEx below fail to correctly match an email address?

- **Groups: Organizing patterns into parts**

- Groups are enclosed using "(...)"
- While whole expression must match, groups are captures individually  
(a match is no longer a string but a tuple of strings, one for each group)
- Groups can be nested, e.g., (...(...)...((...))...)  
(order of groups depends on the order in which the groups "open")

Send an email to `alice@example.org` for more information.



|                  |                               |
|------------------|-------------------------------|
| <b>Match:</b>    | <code>user@example.org</code> |
| <b>Group #1:</b> | <code>alice</code>            |
| <b>Group #2:</b> | <code>example.org</code>      |

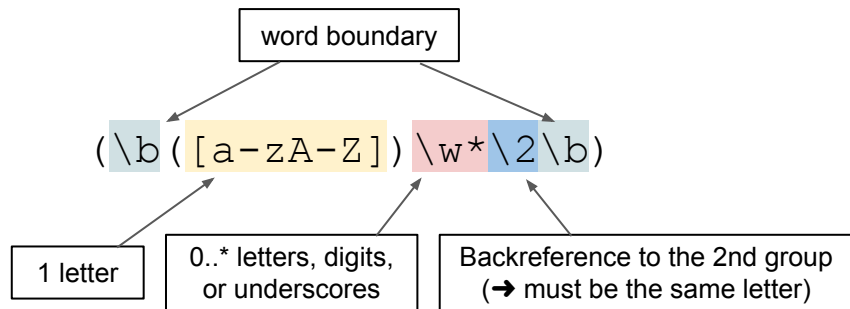
# Backreferences

**Quick quiz:** Can the same be achieved using only 1 group?

- Reference groups within a RegEx
  - Find repeated patterns (see example below)
  - Support only partial replacement of matches

- Example:

- "My *mom* said I need to pass this *test*."
- Goal: Find all words that start and end with the same letter



|                  |            |
|------------------|------------|
| <b>Match:</b>    | <i>mom</i> |
| <b>Group #1:</b> | <i>mom</i> |
| <b>Group #2:</b> | <i>m</i>   |

|                  |             |
|------------------|-------------|
| <b>Match:</b>    | <i>test</i> |
| <b>Group #1:</b> | <i>test</i> |
| <b>Group #2:</b> | <i>t</i>    |

# Lookarounds

- Special groups — assertions

- Match like any other group, but do not capture the match
- 2 types: lookaheads and lookbehinds
- 2 forms of assertion: positive and negative

|       | Type                | Example                                                        |
|-------|---------------------|----------------------------------------------------------------|
| (?=)  | positive lookahead  | A ( =B) → finds expr. A but only when followed by expr. B</td  |
| (?!)  | negative lookahead  | A (?!B) → finds expr. A but only when not followed by expr. B  |
| (?<=) | positive lookbehind | (?<=B) A → finds expr. A but only when preceded by expr. B     |
| (?<!) | negative lookbehind | (?<!B) A → finds expr. A but only when not preceded by expr. B |

# Lookarounds — Example

- Positive lookahead

- *"Paying 10 SGD for 1 kg of chicken seems fair."*
- Goal: Extract all *kg* values (numbers followed by the unit *kg*)

`\d+ ( ?=\s*kg)`



*"Paying 10 SGD for 1 kg of chicken seems fair."*

*"Paying 10 SGD for 1.5 kg of chicken seems fair."*

*"Paying 10 SGD for 1,500.00 kg of chicken seems fair."*

`[0-9.,]*[0-9]+ ( ?=\s*kg)`



*"Paying 10 SGD for 1 kg of chicken seems fair."*

*"Paying 10 SGD for 1.5 kg of chicken seems fair."*

*"Paying 10 SGD for 1,500.00 kg of chicken seems fair."*

# Outline

- **Regular Expressions**

- Basic Concepts
- **Relationship to FSA**
- Error Types

- **Corpus Preprocessing**

- Tokenization
- Normalization
- Stemming / Lemmatization
- Segmentation

- **Word error handling**

- Spelling Errors
- Minimum Edit Distance
- Noisy Channel Model

# Pre-Lecture Activity for Next Week

- **Assigned Task** (due before Jan 20)
  - Post a 1-2 sentence answer to the following question into the L1 Discussion forum (you will find the thread on Canvas > Discussion > Week 2 (L1))

*"What is the relationship between a Finite State Machine and Regular Expressions?"*

**Side notes:**

- This task is meant as a warm-up to provide some context for the next lecture
- No worries if you get lost; we will talk about this in the next lecture
- You can just copy-&-paste others' answers but this won't help you learn better

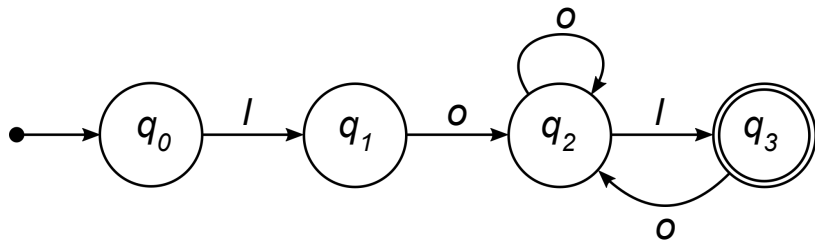


# Relationship to Finite State Automata

- Equivalence

- Regular Expressions describe **Regular Languages**  
(most restricted types of languages w.r.t Chomsky Hierarchy)
- Regular Language = language accepted by a FSA

Example: FSA that accepts the Regular Language described by the Regular Expression  $I(o+I)^+$



Regular Expression

$I(o+I)^+$

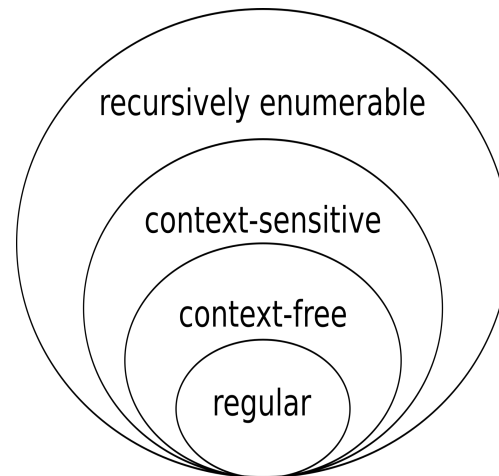


Regular Language

$\{I, Io, Ioo, Iooo, \dots\}$

**Chomsky Hierarchy**

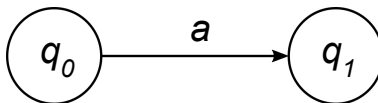
(Source: [Wikipedia](https://en.wikipedia.org/wiki/Chomsky_hierarchy))



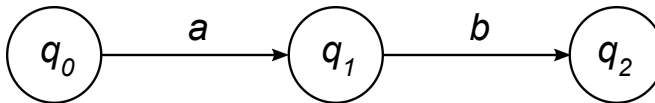
# Relationship to Finite State Automata

- Basic equivalences

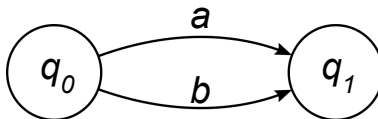
**a**



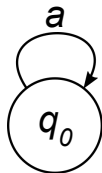
**ab**



**a | b**



**a\***





## In-Lecture Activity (5 mins)



# Outline

- **Regular Expressions**

- Basic Concepts
- Relationship to FSA
- **Error Types**

- **Corpus Preprocessing**

- Tokenization
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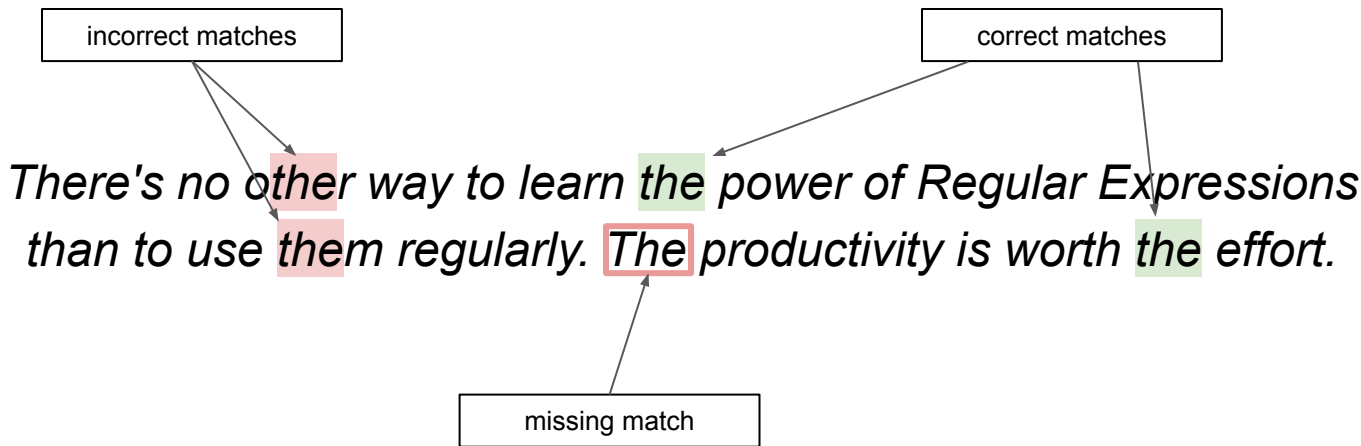
- **Word error handling**

- Spelling Errors
- Minimum Edit Distance
- Noisy Channel Model

# Error Types — What Can Go Wrong

**Quick quiz:** What would be a better RegEx for this task?

- Example: Find all occurrences of article "the"
  - Naive approach: "the" (fixed pattern)



# Error Types

- 2 basic types of errors

Matching strings that we should not have matched  
(e.g., *other*, *theology*, *weather*, *bathe*, *mother*)



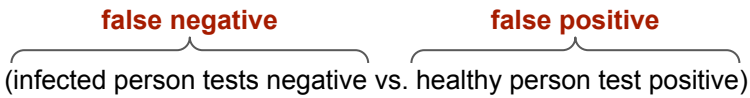
**False Positives**  
(Type I Errors)

Not matching things that we should have matched  
(e.g., *THE*)



**False Negatives**  
(Type II Errors)

# Error Types — Observations

- Many contexts deal with these 2 types of errors, e.g.:
  - Medical testing (e.g., ART test is positive but person is not infected with COVID → false positive)
  - Information retrieval (e.g., a Web search is missing a relevant page → false negative)
  - Document classification (e.g., an abusive tweet has be classified as positive → false positive)
- Reducing errors
  - Both error types not always equally bad   
(infected person tests negative vs. healthy person test positive)
  - Reducing False Positives and False Negatives often in conflict  
(reducing False Positives often increases False Negatives, and vice versa)

# Regular Expressions — Summary

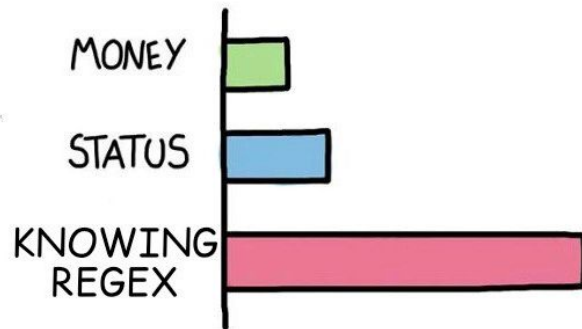
- Know their powers

- Extremely useful tool for many (low-level) text processing tasks (e.g., data preprocessing, tokenization, normalization)
- Important skill for anyone working with strings or text

- Know their limitations

- Regular Expressions represent hard rules
  - Higher-level text processing task generally require statistical models ("soft" rules)
- Machine Learning classifiers

## WHAT GIVES PEOPLE FEELINGS OF POWER



# Outline

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# Tokenization

- Tokenization: splitting a string into **tokens** → **vocabulary** (set of all unique tokens)
  - Token = character sequence with a semantic meaning  
(typically: words, numbers, punctuation — but may differ depending on applications)
  - Very important for step for most NLP algorithms  
(tokenization errors quickly propagate up → "garbage in, garbage out")

Character-based tokenization  
trivial (e.g., using Regex: .)

- 3 basic approaches

|                 |     |    |         |     |      |        |      |       |      |         |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|-----------------|-----|----|---------|-----|------|--------|------|-------|------|---------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| character-based | S   | h  | e       | '   | s    | d      | r    | i     | v    | i       | n | g | f | a | s | t | e | r | t | h | a | n | a | l | l | o | w | e | d | . |
| subword-based   | She | 's | driv    | ing | fast | er     | than | allow | ed   | .       |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| word-based      | She | 's | driving |     |      | faster |      |       | than | allowed |   |   | . |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |

# Tokenization — Word-Based

**Quick quiz:** What is an important assumption for the 2 approaches?

- 2 intuitive approaches (solved using RegEx)

- Match all words, numbers and punctuation marks → `\w+ | \d+ | [ , . ; : ]`
- Match boundaries between "words" and "non-words" → `(?=\W) | (?<=\W)`

`\w+ | \d+ | [ , . ; : ]` → *NLP is fun, and there is so much to learn in 13 weeks.*

`(?=\W) | (?<=\W)` → *NLP|is|fun||and||there|is|so|much|to|learn|in|13|weeks|*

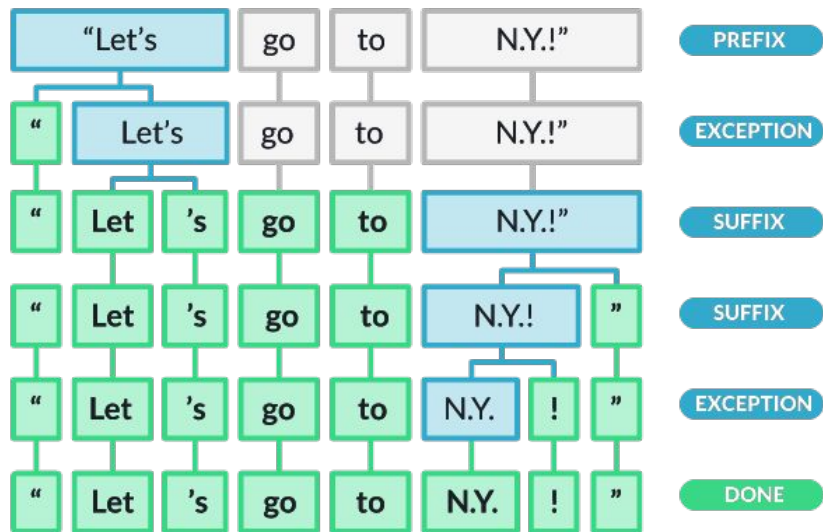
# Tokenization — It Quickly Gets Tricky

- Multiword phrases → *I just came back from New York City.*
- Common contractions → *I'm not home, so don't call.*
- Hyphenations → *NLP is a well-defined but non-trivial topic.*
- Acronyms, names, etc. → *I watched a C++ documentary on T.V.*
- Special tokens → *My email is chris@nus.comp.nus.sg :o)*

RegEx used:

`\w+|\d+|[, .; :]`

# Example: spaCy Tokenizer



- (1) Split string on whitespace characters
- (2) From left to right, recursively check substrings:
  - Does substring match an exception rule?  
(e.g., "don't" → "do", "n't", but keep "U.K.")
  - Can a prefix, suffix or infix be split of?  
(e.g., commas, periods, quotes, hyphens)

Substring checks based on

- Regular Expressions
- Hand-crafted rules / patterns

# Example: Chris's Tokenizer

@ B o b . . . I  # D u n e M o v i e : o ) ) )

@ B o b . . . I  # D u n e M o v i e : o ) ) )

@ B o b . . . I  # D u n e M o v i e : o ) ) )

@ B o b . . . I  # D u n e M o v i e : o ) ) )

@ B o b . . . I  # D u n e M o v i e : o ) ) )

@ B o b . . . I  # D u n e M o v i e : o ) ) )

Sequential labeling of characters

Label all whitespace characters



Label all unicode characters



Label all emoticons



Label all special token types



Label all punctuation marks



Label all alphanumeric characters

→ Tokens = Substrings with adjacent characters with the same labels

# Tokenization — Language Issues

- French

- Different uses of apostrophes and hyphens (compared to English)

direct article

*l'ensemble*

"the whole" / "all"

indicates imperative

*donne-moi*

"give me!"

→ 1 token or 2 tokens?

- German

- Very common: compound nouns

*Arbeiterunfallversicherungsgesetz*

"worker injury insurance act"

→ important: **compound splitter**

# Tokenization — Language Issues

- Languages without whitespaces separating words

## Chinese

莎 拉 波 娃 | 现 在 | 居 住 | 在 | 美 国 | 东 南 部 | 的 | 佛 罗 里 达

" Sharapova now lives in US southeastern Florida "

## Japanese

- multiple syllabaries
- multiple formats for dates and amounts

フォーチュン500社は情報不足のため時間あた\$500K(約6,000万円)

Katakana Hiragana Kanji Romanji

# Tokenization — Word Segmentation of Chinese Text

- Baseline algorithm: **Maximum Matching**



莎拉波娃现在居住在美国东南部的佛罗里达



**莎拉波娃**现在居住在美国东南部的佛罗里达  
*Sharapova*



莎拉波娃|现在居住在美国东南部的佛罗里达

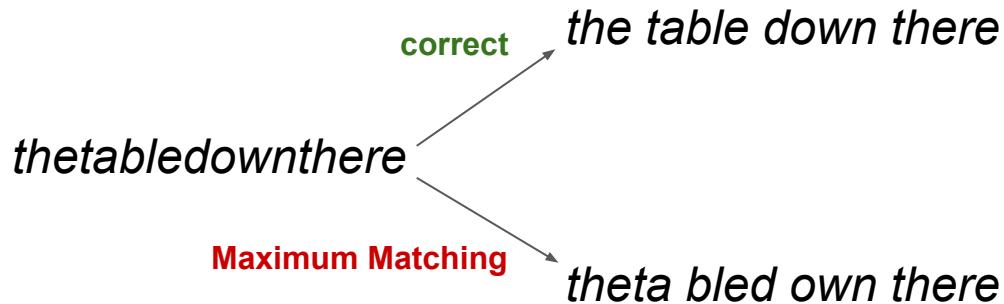


莎拉波娃|**现在**居住在美国东南部的佛罗里达  
*now*

- (1) Place a pointer at the beginning of the string
- (2) Find longest word in dictionary that matches string starting the pointer
- (3) Mover the pointer over the word in the string
- (4) Goto #2 to process the whole string

# Tokenization — Maximum Matching

- Surprisingly good performance on Chinese text  
(even better performance with probabilistic methods or extensions)
- Generally does not work for English text



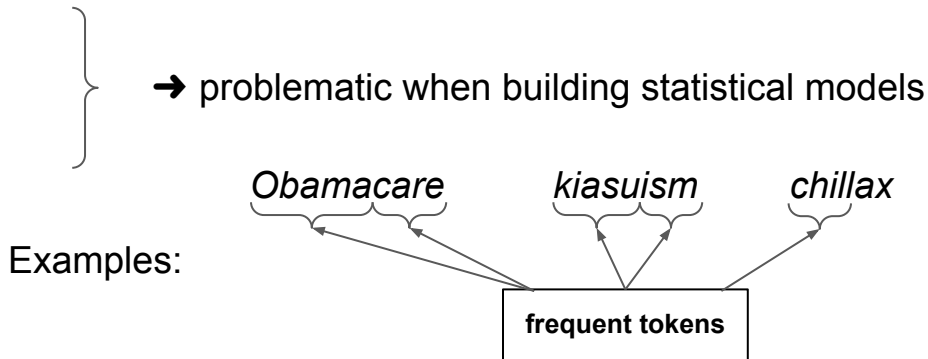
# Tokenization — Subword-Based

- Subword-based tokenization

- So far: a priori specification of rules (e.g., RegEx) what constitutes valid tokens
- Now: use data to specify how to tokenize

- Why do we want to do this?

- **Out Of Vocabulary (OOV)** words  
(word/token an NLP model has not seen before)
- Very rare words in corpus



→ **Goal:** Split OOV and rare words into (some) known & frequent tokens

# Tokenization — Subword-Based

- Different algorithms for subword tokenization
  - Byte-Pair Encoding (BPE), Unigram Language Model Tokenization, WordPiece, etc.
- Different approaches, similar 2-parts setup

(1) **Token Learner**

Takes raw training corpus and induces a vocabulary (i.e., set of tokens)

(2) **Token Segmenter**

Takes a raw text and tokenizes it according to vocabulary

# Tokenization — BPE Token Learner

**Quick quiz:** What happens if  $k=0$  or  $k=\infty$  ?

**Corpus:** *"low low low low low lower lower newest newest newest newest newest newest widest widest widest longer"*

special end-of-word token

Initialize vocabulary (e.g., {'d', 'e', 'g', 'i', 'l', 'n', 'o', 'r', 's', 't', 'w', \_})

## REPEAT

Find the 2 tokens most frequently adjacent to each other (e.g., 'e', 's')

Add a new merged token 'es' to vocabulary

Replace every adjacent 'e' 's' in corpus with 'es'

**UNTIL** k merges have been done

parameter of algorithm

# Tokenization — BPE Token Learner

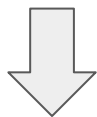
## corpus representation

|   |               |
|---|---------------|
| 6 | n e w e s t _ |
| 5 | l o w _       |
| 3 | w i d e s t _ |
| 2 | l o w e r _   |
| 1 | l o n g e r _ |

## vocabulary

d, e, g, i, l, n, o, r, s, t, w, \_

## merges



most frequent pair: **e** & **s** (9 occurrences)

## corpus representation

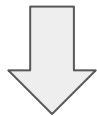
|   |                     |
|---|---------------------|
| 6 | n e w <b>es</b> t _ |
| 5 | l o w _             |
| 3 | w i d <b>es</b> t _ |
| 2 | l o w e r _         |
| 1 | l o n g e r _       |

## vocabulary

d, e, g, i, l, n, o, r, s, t, w, \_, **es**

## merges

**(e, s)**



most frequent pair: **es** & **t** (9 occurrences)

# Tokenization — BPE Token Learner

## corpus representation

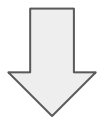
|   |                    |
|---|--------------------|
| 6 | n e w <b>est</b> _ |
| 5 | l o w _            |
| 3 | w i d <b>est</b> _ |
| 2 | l o w e r _        |
| 1 | l o n g e r _      |

## vocabulary

d, e, g, i, l, n, o, r, s, t, w, \_, es, **est**

## merges

(e, s), (**es**, t)



most frequent pair: **est** & \_ (9 occurrences)

## corpus representation

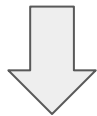
|   |                    |
|---|--------------------|
| 6 | n e w <b>est</b> _ |
| 5 | l o w _            |
| 3 | w i d <b>est</b> _ |
| 2 | l o w e r _        |
| 1 | l o n g e r _      |

## vocabulary

d, e, g, i, l, n, o, r, s, t, w, \_, es, est, **est**\_

## merges

(e, s), (es, t), (**est**, \_)



most frequent pair: **l** & **o** (8 occurrences)

# Tokenization — BPE Token Learner

## corpus representation

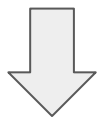
|   |              |
|---|--------------|
| 6 | n e w est_   |
| 5 | lo w _       |
| 3 | w i d est_   |
| 2 | lo w e r _   |
| 1 | lo n g e r _ |

## vocabulary

d, e, g, i, l, n, o, r, s, t, w, \_, es, est, est\_, lo

## merges

(e, s), (es, t), (est, \_), (1, o)



most frequent pair: lo & w (7 occurrences)

## corpus representation

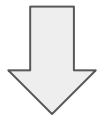
|   |              |
|---|--------------|
| 6 | n e w est_   |
| 5 | low _        |
| 3 | w i d est_   |
| 2 | low e r _    |
| 1 | lo n g e r _ |

## vocabulary

d, e, g, i, l, n, o, r, s, t, w, \_, es, est, est\_, lo, low

## merges

(e, s), (es, t), (est, \_), (1, o), (lo, w)



most frequent pair: n & e (6 occurrences)

# Tokenization — BPE Token Learner

**vocabulary** d, e, g, i, l, n, o, r, s, t, w, \_, es, est, est\_, lo, low, **ne**

**merges** (e, s), (es, t), (est, \_), (l, o), (lo, w), **(n, e)**



**vocabulary** d, e, g, i, l, n, o, r, s, t, w, \_, es, est, est\_, lo, low, ne, **new**

**merges** (e, s), (es, t), (est, \_), (l, o), (lo, w), (n, e), **(ne, w)**



**vocabulary** d, e, g, i, l, n, o, r, s, t, w, \_, es, est, est\_, lo, low, ne, new, **newest\_**

**merges** (e, s), (es, t), (est, \_), (l, o), (lo, w), (n, e), (ne, w), **(new, est\_)**



...

# Tokenization — BPE Token Segmenter

**vocabulary** d, e, g, i, l, n, o, r, s, t, w, \_, es, est, est\_, lo, low, ne, new, newest\_,  
low\_, er, er\_, wi, wid, widest\_, lower\_, lon, long, longer\_

**merges** (e, s), (es, t), (est, \_), (l, o), (lo, w), (n, e), (ne, w), (new, est\_), (low, \_), (e, r),  
(er, \_), (w, i), (wi, d), (wid, est\_), (low, er\_), (lo, n), (lon, g), (long, er\_)

Tokenize/segment  
*"newer"*

Run each merge in order  
they have been learned

n e w e r \_  
ne w e r \_  
new e r \_  
new er \_  
new er \_

(n, e)  
(ne, w)  
(e, r)  
(er, \_)

→ tokens: "new", "er\_"

# Tokenization — Summary

- Tokenization as low-level NLP task
  - Challenges: important, non-trivial, language-dependent
  - Particularly tricky for informal language (e.g., social media)
- 3 basic approaches
  - Character-based (trivial to do but often not suitable — individual characters generally carry no semantic meaning)
  - Word-based (a priori specification of rules; language-dependent; problem: OOV/rare words)
  - Subword-based (tokenization learned from data — tokens are often morphemes!)
- Practical consideration (when using off-the-shell word-based tokenizers)
  - What is my type of text (e.g., formal or informal)? Are there special tokens (e.g., URLs, hashtags)?
  - Try and assess different tokenizers — very, very last resort: write your own tokenizer

# Outline

- Regular Expressions
  - Basic Concepts
  - Relationship to FSA
  - Error Types
- **Corpus Preprocessing**
  - Tokenization
  - **Normalization**
  - Stemming / Lemmatization
  - Segmentation
- Word error handling
  - Spelling Errors
  - Minimum Edit Distance
  - Noisy Channel Model

# Normalization

- Goal: Convert text into a canonical (standard) form
  - Remove noise / "randomness" from text
  - Affects characters, words, sentences, documents
- Implicit definition of equivalence classes
  - Suitable normalization steps depend on task/application

Alternative to equivalence classes: **asymmetric expansion**

Example: Web Search (utilize case of search terms)

## Entered term

## Searched terms

|         |   |                          |
|---------|---|--------------------------|
| window  | → | window, windows          |
| windows | → | Windows, windows, window |
| Windows | → | Windows                  |

| Raw                                                          | Normalized |
|--------------------------------------------------------------|------------|
| Germany<br>GERMANY                                           | germany    |
| USA<br>U.S.A<br>US of A                                      | USA        |
| tonight<br>tonite<br>2N8                                     | tonight    |
| connect<br>connects<br>connected<br>connecting<br>connection | connect    |
| :)<br>:-)<br>:o)                                             | smile      |

# Normalization — Case Folding

- When to fold?

- Common application: Information Retrieval  
(e.g., Web search where most users type only in lowercase anyway)
- Potential problems: *Bush* vs. *bush*, *MOM* vs. *mom*, *Cloud* vs. *cloud*, etc.  
(potential exception: upper case word in mid sentence?)

- When NOT to fold?

- NLP tasks where case of letters or words are important features
- Examples: Named Entity Recognition, Machine Translation

*They sent **us** a card from the **US** during their vacation.*

Distinction important for NER and MT!

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# Normalization — Stemming & Lemmatization

- Motivating example:

*"dogs make the best friends"* vs. *"a dog makes a good friend"*

→ Very similar semantics but (very) different syntax

- Common reasons for variations of the same word

- Singular vs. plural form (mainly of nouns)
- Different tenses of verbs
- Comparative/superlative of adjectives

→ Can we normalize words to abstract from such variations?

# Normalization — Stemming

- Idea of Stemming

- Reduce words to their stem
- Approach: crude chopping of affixes based on rules (→ language dependent)
- Different stemmers apply different rules

- Characteristics

- Pro: fast + no lexicon required
- Con: stemmed word not necessarily a proper word (i.e., not in dictionary)

## Examples

(alternatives reflect results from different stemmers)

| Raw               | Stemmed        |
|-------------------|----------------|
| <i>cats</i>       | <i>cat</i>     |
| <i>running</i>    | <i>run</i>     |
| <i>phones</i>     | <i>phon(e)</i> |
| <i>presumably</i> | <i>presum</i>  |
| <i>crying</i>     | <i>cry/cri</i> |
| <i>went</i>       | <i>went</i>    |
| <i>worse</i>      | <i>wors</i>    |
| <i>best</i>       | <i>best</i>    |
| <i>mice</i>       | <i>mic(e)</i>  |

# Normalization — Stemming: Porter Stemmer

- Porter Stemmer — most common stemmer for English text
  - Simple, efficient + very good results in practice
- Series of rewrite rules that run in a cascade
  - Output of each pass is fed is input to the next pass
  - Stemming stops if a pass yields no more changes

|                              |                |                                                                                               |
|------------------------------|----------------|-----------------------------------------------------------------------------------------------|
|                              | sses → ss      | e.g.: <i>possesses</i> → <i>possess</i> , <i>classes</i> → <i>class</i>                       |
|                              | tional → tion  | e.g., <i>optional</i> → <i>option</i> , <i>fictional</i> → <i>function</i>                    |
|                              | ies → i        | e.g., <i>cries</i> → <i>cri</i> , <i>tries</i> → <i>tri</i>                                   |
| stem must contain vowel →    | (*v*)ing → ε   | e.g.: <i>sing</i> → <i>sing</i> , <i>singing</i> → <i>sing</i> , <i>talking</i> → <i>talk</i> |
| stem must contain >1 chars → | (m>1)ement → ε | e.g., <i>replacement</i> → <i>replac</i> , <i>cement</i> → <i>cement</i>                      |

# Normalization — Lemmatization

- Idea of Lemmatization

- Reduce inflections or variant forms to base form
- Find the correct dictionary headword form
- Differentiates between word forms: nouns (N), verbs (V), adjectives (A)

| Raw            | Lemmatized (N) | Lemmatized (V) | Lemmatized (A) |
|----------------|----------------|----------------|----------------|
| <i>running</i> | <i>running</i> | <i>run</i>     | <i>running</i> |
| <i>phones</i>  | <i>phone</i>   | <i>phone</i>   | <i>phones</i>  |
| <i>went</i>    | <i>went</i>    | <i>go</i>      | <i>went</i>    |
| <i>worse</i>   | <i>worse</i>   | <i>worse</i>   | <i>bad</i>     |
| <i>mice</i>    | <i>mouse</i>   | <i>mice</i>    | <i>mice</i>    |

# Normalization — Lemmatization: Characteristics

- Pros

- Lemmatized words are proper words (i.e., dictionary words)
- Can normalize irregular forms (e.g., *went* → *go*, *worst* → *bad*)

- Cons

- Requires curated lexicons / lookup tables + rules (typically)
- Requires Part-of-Speech tags for correct results
- Generally slower as stemming

# Normalization — Stemming & Lemmatization

- Back to our motivating example

**Raw:**       *"dogs make the best friends"*

*"a dog makes a good friend"*

**Stemmed:**       *"dog make the best friend"*

*"a dog make a good friend"*

**Lemmatized:**       *"dog make the good friend"*

*"a dog make a good friend"*

# Normalization — Final Words

- Canonical form also effects tokenization, e.g.: Penn Treebank Tokenizer
  - Separate out clitics (e.g., *doesn't* → *does n't*; *John's* → *John 's*)
  - Keep hyphenated words together
  - Separate out all punctuation symbols
- Other common normalization steps
  - Removal of stopwords (e.g., *a*, *an*, *the*, *not*, *and*, *or*, *but*, *to*, *from*, *at*)
  - Removal of non-standard tokens (e.g., URs, emojis, emoticons)
  - ...



## Quick Quiz



# Outline

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# Sentence Segmentation

- Sound like a simple task but...

- Period "." can be quite ambiguous (e.g., "1.25", "U.S.A.", "Dr.") — "?", "!" relatively unambiguous
- Poor punctuation in informal text (common: missing whitespaces, missing capitalization)

→ RegEx for segmenting sentences quickly become very complex

Example RegEx: `(?<!\w\.\w.)(?<![A-Z][a-z]\.)(?<=\.|\?)\s`

(Source: [Stackoverflow](#))

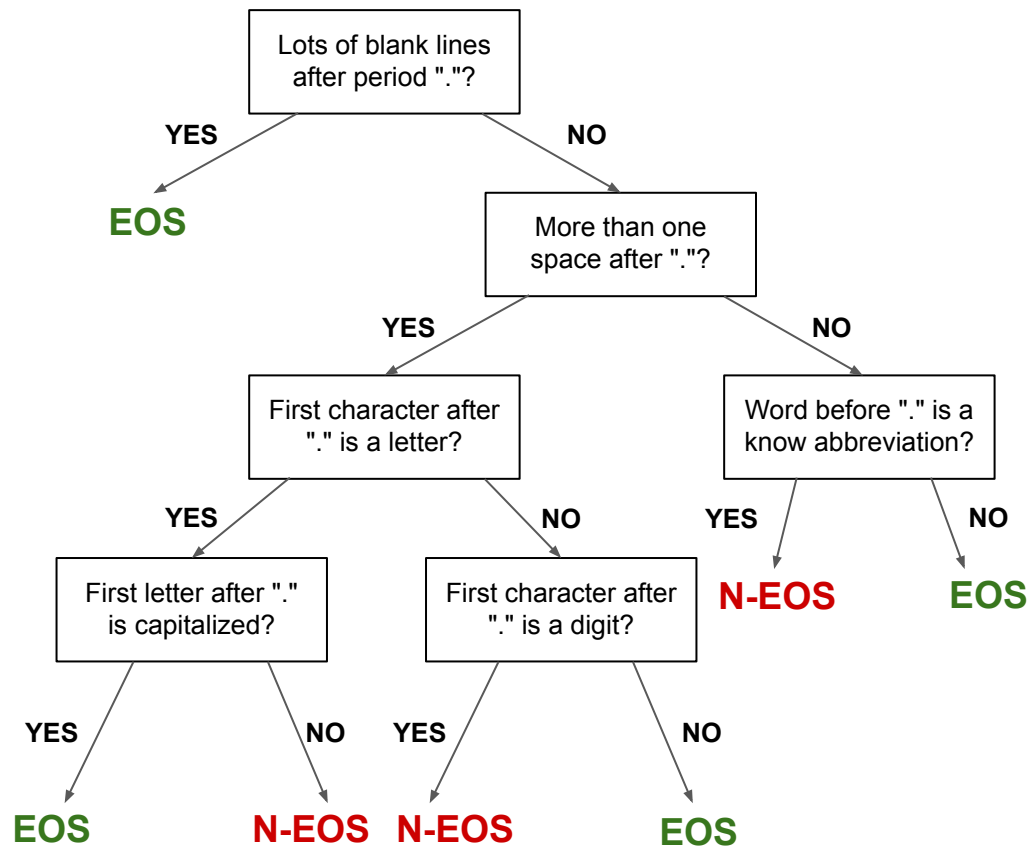
- Alternative: binary classifier

- Consider each period "." in a text
- Classify: **EndOfSentence** or **NotEndOfSentence**

→ Possible approaches: handwritten rules, set of RegEx, machine learning

# Example: Simple Rules (represented as a binary Decision Tree)

**Quick quiz:** What are some common cases where this classifier would fail?



# Many Other Features Conceivable

- Example: numerical features
  - length of word before / after period "."
  - Distance (in #chars) to next punctuation mark
  - Probabilities derived from a dataset  
(e.g., probability of with "." occurs at the end of sentence)

**Side note:** In informal text (e.g., social media) people often use emoticons or emojis to separate sentences, making this task even more complicated.

# Break



Most relevant ▼



Nisha Virani

I am completely losing my mind

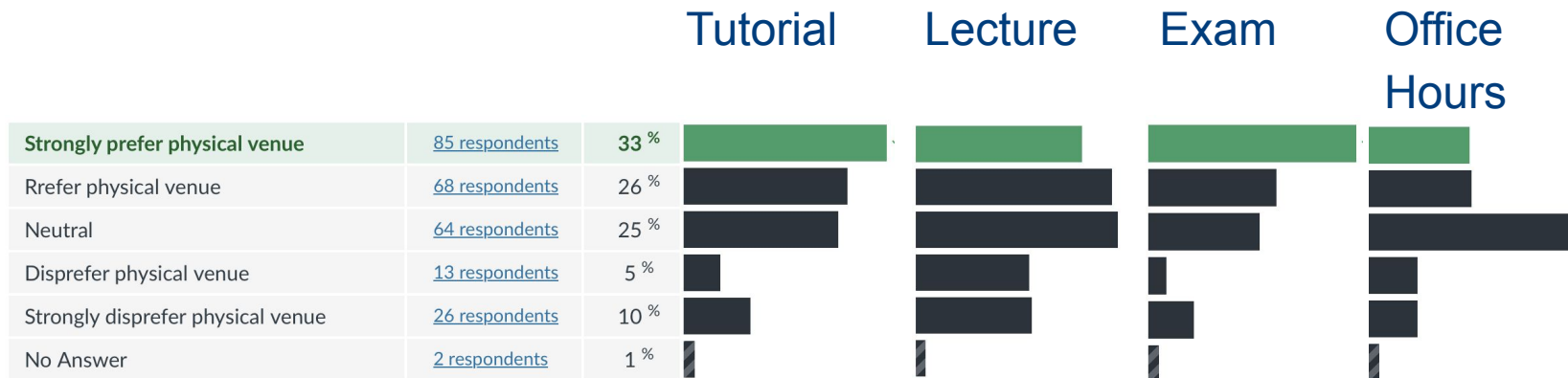
help me 🙏🙏🙏🙏🙏🙏🙏🙏🙏🙏

That's what artificial intelligence  
do for you. I thought it's a joke, but

# Why are you taking this module?

|                                                                                                           |                 |      |                                                                                      |
|-----------------------------------------------------------------------------------------------------------|-----------------|------|--------------------------------------------------------------------------------------|
| <b>It's a core requirement of my programme.</b>                                                           | 23 respondents  | 9 %  |   |
| It's an elective course (one of a basket) requirement for my programme.                                   | 103 respondents | 40 % |   |
| I need this course to graduate this coming semester.                                                      | 55 respondents  | 21 % |   |
| I'm taking a related focus area, minor or track that has this as part of the possible fulfilling courses. | 139 respondents | 54 % |   |
| I'm a student doing research, and NLP is my research area or related to my research area.                 | 24 respondents  | 9 %  |   |
| It looked interesting.                                                                                    | 214 respondents | 83 % |   |
| I have friends that are taking this course.                                                               | 70 respondents  | 27 % |   |
| It fits well in my timetable.                                                                             | 52 respondents  | 20 % |   |
| Someone referred me to take this course because of its content.                                           | 29 respondents  | 11 % |   |
| Someone referred me to take this course because of its instruction staff.                                 | 26 respondents  | 10 % |   |
| I like project courses.                                                                                   | 40 respondents  | 16 % |   |
| I saw that it was popular.                                                                                | 30 respondents  | 12 % |   |
| I have fulfilled all the prerequisites for the course, so why not?                                        | 38 respondents  | 15 % |   |
| Others, I've mentioned in the next question.                                                              | 5 respondents   | 2 %  |  |

# Venues



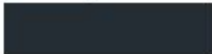
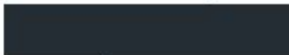
# Major or Programme

|                                      |                 |      |   |
|--------------------------------------|-----------------|------|---|
| Arts                                 |                 | 0 %  | ✓ |
| Business                             | 9 respondents   | 3 %  |   |
| Computer Engineering                 | 20 respondents  | 8 %  |   |
| Computer Sciences                    | 175 respondents | 68 % |   |
| Data Science                         | 51 respondents  | 20 % |   |
| English Language, Foreign Language   |                 | 0 %  |   |
| Linguistics                          |                 | 0 %  |   |
| Math / Statistics                    | 22 respondents  | 9 %  |   |
| Masters                              | 42 respondents  | 16 % |   |
| Ph.D. Candidate                      |                 | 0 %  |   |
| SCALE / Continuing Education Learner |                 | 0 %  |   |
| Other                                | 6 respondents   | 2 %  |   |

# Overseas?

|                                              |                 |      |                                                                                     |
|----------------------------------------------|-----------------|------|-------------------------------------------------------------------------------------|
| Yes, abroad on exchange or NOC.              | 1 respondent    | 0 %  |  |
| Yes, on internship.                          | 25 respondents  | 10 % |  |
| Considering one of the two above.            | 13 respondents  | 5 %  |  |
| No, full-time local student (most students). | 219 respondents | 85 % |  |

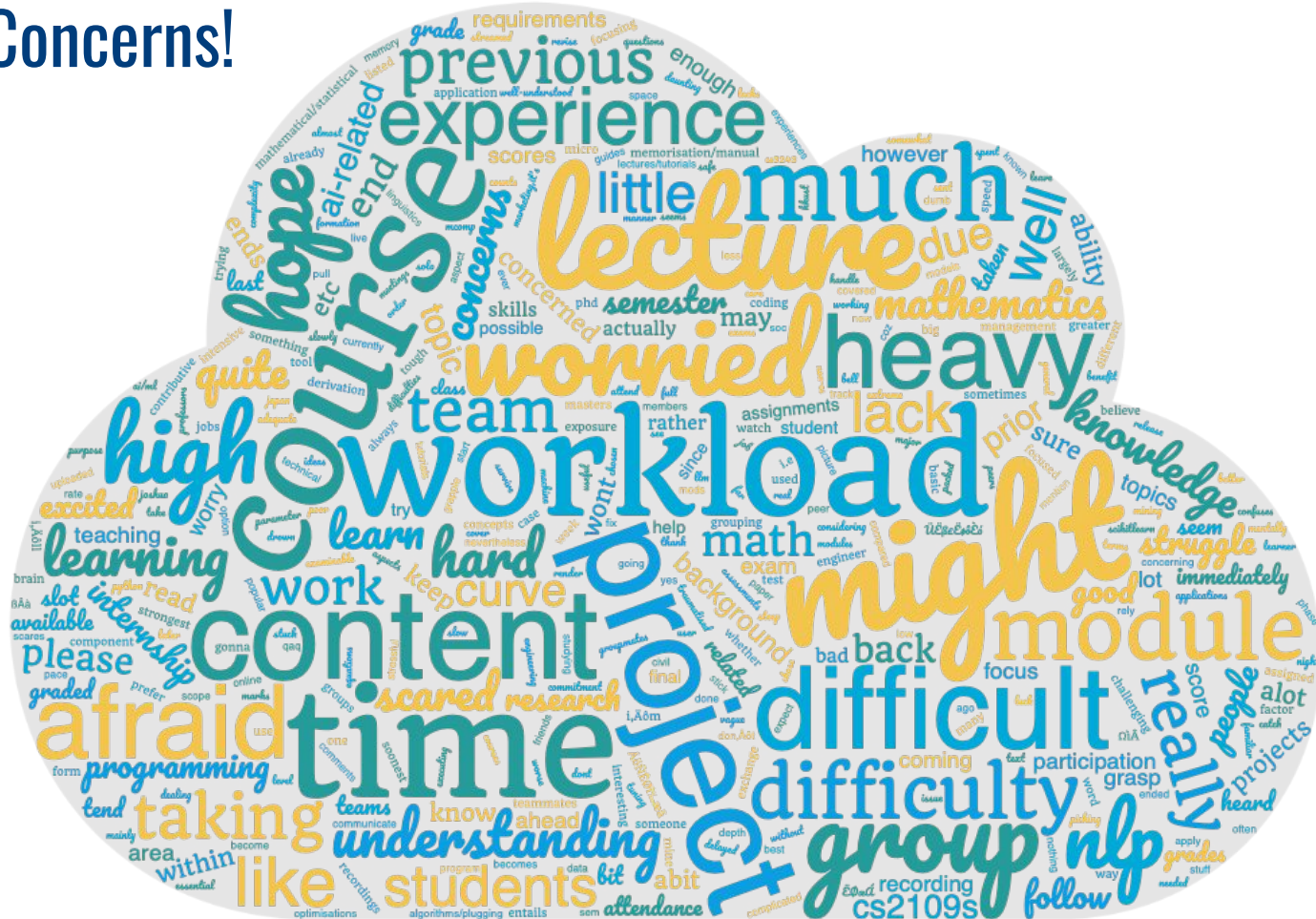
# NLP Career Path

|                    |                 |      |                                                                                     |
|--------------------|-----------------|------|-------------------------------------------------------------------------------------|
| No idea.           | 16 respondents  | 6 %  |  |
| Unlikely.          | 9 respondents   | 3 %  |  |
| Somewhat Unlikely. | 29 respondents  | 11 % |  |
| So-So.             | 72 respondents  | 28 % |  |
| Somewhat Likely.   | 100 respondents | 39 % |  |
| Likely.            | 31 respondents  | 12 % |  |
| No Answer          | 1 respondent    | 0 %  |  |

# What do you want to learn?



# Your Concerns!



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# Spelling Errors

Increasing Complexity

## 1. Non-word error detections

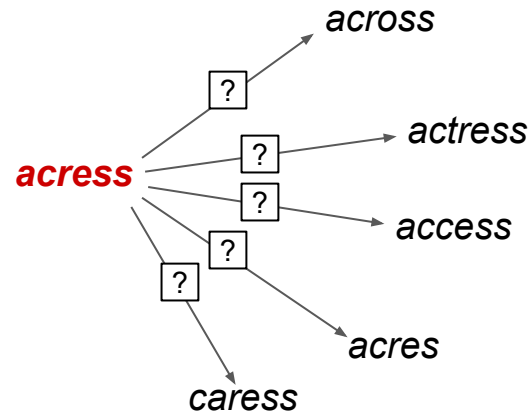
- Basically, word is not found in dictionary
- Example: detecting *graffe* (misspelling of *giraffe*)

## 2. Isolated-word error correction

- Consider word in isolation (i.e., without surrounding words)
- Example: correcting *graffe* to *giraffe*

## 3. Context-sensitive error detection & correction

- Consider surrounding words to detect and correct errors
- Important for "wrong" words that are spelled correctly
- Examples: *there* vs. *three*, *dessert* vs. *desert*, *son* vs. *song*



# Spelling Errors — Common Patterns

- Observation

- Most misspelled words in typewritten text are **single-error**
- Damerau (1964): 80%, Peterson (1986): 93-95%

- Single-error misspellings

- Insertion (e.g., *acress* vs. *acres*)
- Deletion (e.g., *acress* vs. *actress*)
- Substitution (e.g., *acress* vs. *access*)
- Transposition (e.g., *acress* vs. *caress*)

For non-word errors:

- Good candidates are orthographically similar
- **Minimum Edit Distance**

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# Minimum Edit Distance (MED)

- Minimum Edit Distance between 2 strings  $s_1$  and  $s_2$ 
  - Minimum number of allowed edit operations to transform  $s_1$  into  $s_2$

■ Allowed edit operations: Insertion, Deletion, Substitution, Transposition

Not covered here to keep examples simple

- Example

■  $s_1 = \text{"LANGUAGE"}$

■  $s_2 = \text{"SAUSAGE"}$

→ Alignment of MED:

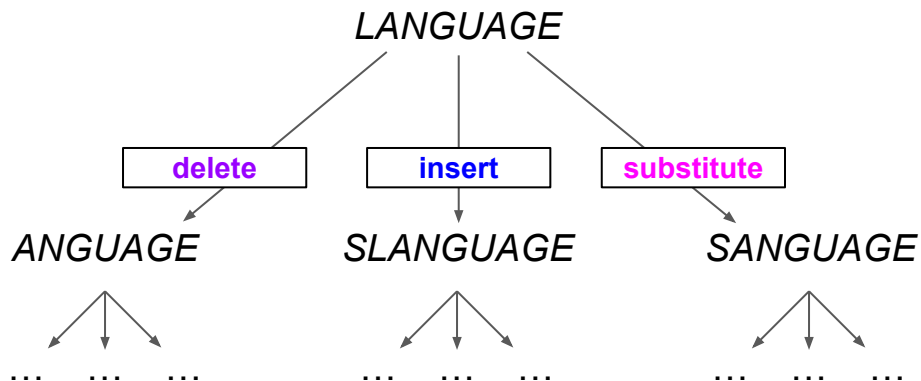
|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| L | A | N | G | U | * | A | G | E |
|   |   |   |   |   |   |   |   |   |
| S | A | * | * | U | S | A | G | E |

MED if all operations cost 1 → 4

MED if Substitution costs 2,  
Insertion 1, Deletion 1 → 5

# Minimum Edit Distance — Calculation

- Problem formulation: Find a path (i.e., sequence of edits) from start string to final string
  - **Initial state:** the word being transformed (e.g., "LANGUAGE")
  - **Target state:** the word being transformed into (e.g., "SAUSAGE")
  - **Operators:** insert, delete, substitute
  - **Path cost:** aggregated costs of all edits



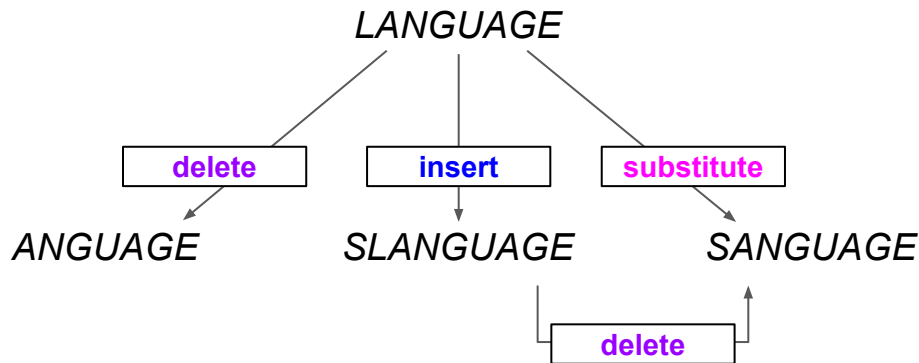
→ Potentially huge search space

→ Naive navigation of all path impractical

# Minimum Edit Distance — Calculation

- Observations

- Many distinct paths end up in the same state



→ No need to keep track of all paths

→ Only important: "cheapest" path to each revisited state  
(best in terms of costs, not just number of operations!)

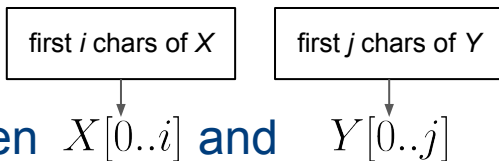
→ Solve using **Dynamic Programming**

solving problems by combining solutions to subproblems

# Minimum Edit Distance — Calculation

- Input: 2 strings

- Source string  $X$  of length  $n$
- Target string  $Y$  of length  $m$



- Define  $D(i, j)$  as MED between  $X[0..i]$  and  $Y[0..j]$

→ MED between  $X$  and  $Y$  is thus  $D(n, m)$

- Bottom-up approach of Dynamic Programming

- Compute  $D(i, j)$  for small  $i, j$  (base cases)
- Compute  $D(i, j)$  for larger  $i, j$  based on previously computes  $D(i, j)$  for smaller  $i, j$

# Minimum Edit Distance — Calculation

- Initialization of bases cases

- $D(i, 0) = i$  (getting from  $X[0..i]$  to empty target string requires  $i$  deletions)
- $D(0, j) = j$  (getting from empty source string to  $Y[0..j]$  requires  $j$  insertions)

- For  $0 < i \leq n$  and  $0 < j \leq m$

$$D(i, j) = \min \begin{cases} D(i-1, j) + 1 & \text{Delete} \\ D(i, j-1) + 1 & \text{Insert} \\ D(i-1, j-1) + \begin{cases} 2, & \text{if } X[i] \neq Y[j] \\ 0, & \text{if } X[i] = Y[j] \end{cases} & \text{Substitute} \end{cases}$$

Assumptions for costs

**Insert:** 1

**Delete:** 1

**Substitute:** 2

→ Levenshtein MED

Complexity analysis

Space:  $O(nm)$

Time:  $O(nm)$

# Minimum Edit Distance — Calculation Example

|          |          |          |          |                                                                                                                                                                                                                                                |          |          |          |          |  |  |  |  |  |  |  |  |  |
|----------|----------|----------|----------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|----------|----------|----------|--|--|--|--|--|--|--|--|--|
| <b>E</b> | 8        |          |          | $D(i, j) = \min \begin{cases} D(i - 1, j) + 1 & \text{Delete} \\ D(i, j - 1) + 1 & \text{Insert} \\ D(i - 1, j - 1) + \begin{cases} 2, & \text{if } X[i] \neq Y[i] \\ 0, & \text{if } X[i] = Y[i] \end{cases} & \text{Substitute} \end{cases}$ |          |          |          |          |  |  |  |  |  |  |  |  |  |
| <b>G</b> | 7        |          |          |                                                                                                                                                                                                                                                |          |          |          |          |  |  |  |  |  |  |  |  |  |
| <b>A</b> | 6        |          |          |                                                                                                                                                                                                                                                |          |          |          |          |  |  |  |  |  |  |  |  |  |
| <b>U</b> | 5        |          |          |                                                                                                                                                                                                                                                |          |          |          |          |  |  |  |  |  |  |  |  |  |
| <b>G</b> | 4        |          |          |                                                                                                                                                                                                                                                |          |          |          |          |  |  |  |  |  |  |  |  |  |
| <b>N</b> | 3        |          |          |                                                                                                                                                                                                                                                |          |          |          |          |  |  |  |  |  |  |  |  |  |
| <b>A</b> | 2        |          |          |                                                                                                                                                                                                                                                |          |          |          |          |  |  |  |  |  |  |  |  |  |
| <b>L</b> | 1        |          |          |                                                                                                                                                                                                                                                |          |          |          |          |  |  |  |  |  |  |  |  |  |
| <b>#</b> | 0        | 1        | 2        | 3                                                                                                                                                                                                                                              | 4        | 5        | 6        | 7        |  |  |  |  |  |  |  |  |  |
|          | <b>#</b> | <b>S</b> | <b>A</b> | <b>U</b>                                                                                                                                                                                                                                       | <b>S</b> | <b>A</b> | <b>G</b> | <b>E</b> |  |  |  |  |  |  |  |  |  |

## Minimum Edit Distance — Calculation Example

|          |          |          |          |          |          |          |          |          |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| <b>E</b> | 8        | 9        | 8        | 7        | 8        | 7        | 6        | 5        |
| <b>G</b> | 7        | 8        | 7        | 6        | 7        | 6        | 5        | 6        |
| <b>A</b> | 6        | 7        | 6        | 5        | 6        | 5        | 6        | 7        |
| <b>U</b> | 5        | 6        | 5        | 4        | 5        | 6        | 7        | 8        |
| <b>G</b> | 4        | 5        | 4        | 5        | 6        | 7        | 6        | 7        |
| <b>N</b> | 3        | 4        | 3        | 4        | 5        | 6        | 7        | 8        |
| <b>A</b> | 2        | 3        | 2        | 3        | 4        | 5        | 6        | 7        |
| <b>L</b> | 1        | 2        | 3        | 4        | 5        | 6        | 7        | 8        |
| <b>#</b> | 0        | 1        | 2        | 3        | 4        | 5        | 6        | 7        |
|          | <b>#</b> | <b>S</b> | <b>A</b> | <b>U</b> | <b>S</b> | <b>A</b> | <b>G</b> | <b>E</b> |

# Minimum Edit Distance — Backtrace & Alignments

- Current limitation

- Base algorithm only returns the MED
- Often important: alignment between strings

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| L | A | N | G | U | * | A | G | E |
|   |   |   |   |   |   |   |   |   |
| S | A | * | * | U | S | A | G | E |

How do we get this?

- Keep track of backtrace

- Remember from which "direction" we entered a new cell
- At the end, trace path from upper right corner to read of alignment

Keep set of pointers  
for each  $i, j$

Small extension to base algorithm:

$$PTR(i, j) = \begin{cases} \text{LEFT} & \text{Insert} \\ \text{DOWN} & \text{Delete} \\ \text{DIAG} & \text{Substitute} \end{cases}$$

**Note:** Backtraces are generally not unique → different alignments for the same MED possible

# Minimum Edit Distance — Backtrace & Alignments

|          |          |          |          |          |          |          |          |          |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| <b>E</b> | 8        | ↖←↓ 9    | ↓ 8      | ↓ 7      | ↖←↓ 8    | ↓ 7      | ↓ 6      | ↖ 5      |
| <b>G</b> | 7        | ↖←↓ 8    | ↓ 7      | ↓ 6      | ↖←↓ 7    | ↓ 6      | ↖ 5      | ← 6      |
| <b>A</b> | 6        | ↖←↓ 7    | ↖↓ 6     | ↓ 5      | ↖←↓ 6    | ↖ 5      | ← 6      | ← 7      |
| <b>U</b> | 5        | ↖←↓ 6    | ↓ 5      | ↖ 4      | ← 5      | ← 6      | ←↓ 7     | ↖←↓ 8    |
| <b>G</b> | 4        | ↖←↓ 5    | ↓ 4      | ↖←↓ 5    | ↖←↓ 6    | ↖←↓ 7    | ↖ 6      | ← 7      |
| <b>N</b> | 3        | ↖←↓ 4    | ↓ 3      | ↖←↓ 4    | ↖←↓ 5    | ↖←↓ 6    | ↖←↓ 7    | ↖←↓ 8    |
| <b>A</b> | 2        | ↖←↓ 3    | ↖ 2      | ← 3      | ← 4      | ↖← 5     | ← 6      | ← 7      |
| <b>L</b> | 1        | ↖←↓ 2    | ↖←↓ 3    | ↖←↓ 4    | ↖←↓ 5    | ↖←↓ 6    | ↖←↓ 7    | ↖←↓ 8    |
| <b>#</b> | 0        | 1        | 2        | 3        | 4        | 5        | 6        | 7        |
|          | <b>#</b> | <b>S</b> | <b>A</b> | <b>U</b> | <b>S</b> | <b>A</b> | <b>G</b> | <b>E</b> |

**Quick quiz:** Why do we choose the diagonal path here?

**L A N G U \* A G E**  
 | | | | | | | |  
**S A \* \* U S A G E**

Complexity analysis

Time:  $O(n+m)$

## Minimum Edit Distance — More Examples

- Biology: Align 2 sequences of nucleotides

AGGCTATCACCTGACCTCCAGGCCGATGCC

TAGCTATCACGACCGCGGTCGATTTGCCCGAC

|   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|----|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| C | 30 | 1 | 30 | 1 | 29 | 1 | 28 | 1 | 27 | 1 | 26 | 1 | 25 | 1 | 24 | 1 | 23 | 1 | 22 | 1 | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9 | 1 | 8 | 1 | 7 | 1 | 6 | 1 | 5 | 1 | 4 | 1 | 3 | 1 | 2 | 1 | 1 |
| G | 28 | 1 | 29 | 1 | 28 | 1 | 27 | 1 | 26 | 1 | 25 | 1 | 24 | 1 | 23 | 1 | 22 | 1 | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8 | 1 | 7 | 1 | 6 | 1 | 5 | 1 | 4 | 1 | 3 | 1 | 2 | 1 | 1 |   |   |
| C | 29 | 1 | 28 | 1 | 27 | 1 | 26 | 1 | 25 | 1 | 24 | 1 | 23 | 1 | 22 | 1 | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7 | 1 | 6 | 1 | 5 | 1 | 4 | 1 | 3 | 1 | 2 | 1 | 1 |   |   |   |   |
| G | 28 | 1 | 27 | 1 | 26 | 1 | 25 | 1 | 24 | 1 | 23 | 1 | 22 | 1 | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6 | 1 | 5 | 1 | 4 | 1 | 3 | 1 | 2 | 1 | 1 |   |   |   |   |   |   |
| T | 27 | 1 | 26 | 1 | 25 | 1 | 24 | 1 | 23 | 1 | 22 | 1 | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5 | 1 | 4 | 1 | 3 | 1 | 2 | 1 | 1 |   |   |   |   |   |   |   |   |
| A | 26 | 1 | 25 | 1 | 24 | 1 | 23 | 1 | 22 | 1 | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4 | 1 | 3 | 1 | 2 | 1 | 1 |   |   |   |   |   |   |   |   |   |   |
| G | 25 | 1 | 24 | 1 | 23 | 1 | 22 | 1 | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3 | 1 | 2 | 1 | 1 |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 24 | 1 | 23 | 1 | 22 | 1 | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2 | 1 | 1 |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 23 | 1 | 22 | 1 | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1 |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| G | 22 | 1 | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| G | 21 | 1 | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 20 | 1 | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| A | 19 | 1 | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 18 | 1 | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| T | 17 | 1 | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 16 | 1 | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 15 | 1 | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| A | 14 | 1 | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| T | 13 | 1 | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| T | 12 | 1 | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 11 | 1 | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 10 | 1 | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| A | 9  | 1 | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 8  | 1 | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| T | 7  | 1 | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| A | 6  | 1 | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| T | 5  | 1 | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 4  | 1 | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| C | 3  | 1 | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| A | 2  | 1 | 1  |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| G | 1  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # | 0  | 1 |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
| # |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |

\* A G G C T A T C A C C T G A C C T C C A G G C C G A \* \* T G \* C C \* \* C  
 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |  
 T A \* G C T A T C A \* C \* G A C C \* G C \* G G T C G A T T T G C C C G A C



# In-Lecture Activity (5 mins)





# In-Lecture Activity (5 mins)



# Minimum Edit Distance — Other Uses in NLP

- Evaluating Machine Translation and speech recognition

e.g., How similar are 2 translations?

|             |           |          |     |        |            |         |     |      |      |
|-------------|-----------|----------|-----|--------|------------|---------|-----|------|------|
| Reference:  | Spokesman | confirms | *   | senior | government | adviser | was | shot | *    |
|             |           |          |     |        |            |         |     |      |      |
| Prediction: | Spokesman | said     | the | senior | *          | adviser | was | shot | dead |

- Named Entity Extraction and Entity Coreference

"We stayed at the \* Merchant Court prior to a cruise"

"The Swissotel Merchant Court is a great place to stay in Singapore"

↑  
Referring to the same entity?

# Minimum Edit Distance — Efficiency

- Time:
- Space:
- Backtrace:

# Minimum Edit Distance — Efficiency



# Minimum Edit Distance — Extensions

- **Weighted Minimum Edit Distance**, e.g.:
  - Spell Correction: some letters are more likely to be mistyped than others
  - Biology: certain kinds of deletions or insertions are more likely than others

## → Generalization of algorithm

- Application-dependent weights (i.e., costs for edit operations)

**Initialization of base cases:**

$$D(0, 0) = 0$$

$$D(i, 0) = D(i - 1, 0) + \text{del}(X[i]), \quad \text{for } 1 < i \leq n$$

$$D(0, j) = D(0, j - 1) + \text{ins}(Y[j]), \quad \text{for } 1 < j \leq m$$

**Recurrence relation:**

$$D(i, j) = \min \begin{cases} D(i - 1, j) & + \text{del}(X[i]) \\ D(i, j - 1) & + \text{ins}(Y[j]) \\ D(i - 1, j - 1) & + \text{sub}(X[i], Y[j]) \end{cases}$$

# Minimum Edit Distance — Extensions

- Needleman-Wunsch

- No penalty for gaps (\*) at the beginning or the end of an alignment
- Good if strings have very different lengths

- Smith-Wasserman

- Ignore badly aligned regions
- Find optimal local alignments within substrings  
(Levenshtein finds the best global distance and alignment)

Common application:  
Alignment of nucleotides sequences

# Outline

- Regular Expressions
  - Basic Concepts
  - Relationship to FSA
  - Error Types
- Corpus Preprocessing
  - Tokenization
  - Normalization
  - Stemming / Lemmatization
  - Segmentation
- Word error handling
  - Spelling Errors
  - Minimum Edit Distance
  - **Noisy Channel Model**

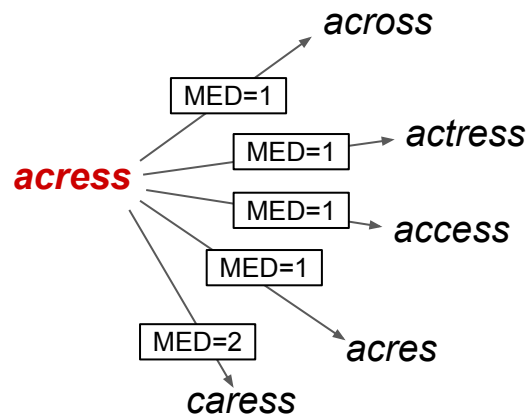
# Where We are Right Now

- Given a misspelled word, generate suitable candidates for error correction

- 80% of errors are within minimum edit distance 1
- Almost all errors within minimum edit distance 2
- Covers also missing spaces and hyphens  
(e.g., *thisidea* vs. *this idea*; *inlaw* vs. *in-law*)

- Still missing: Which is the most likely candidate?

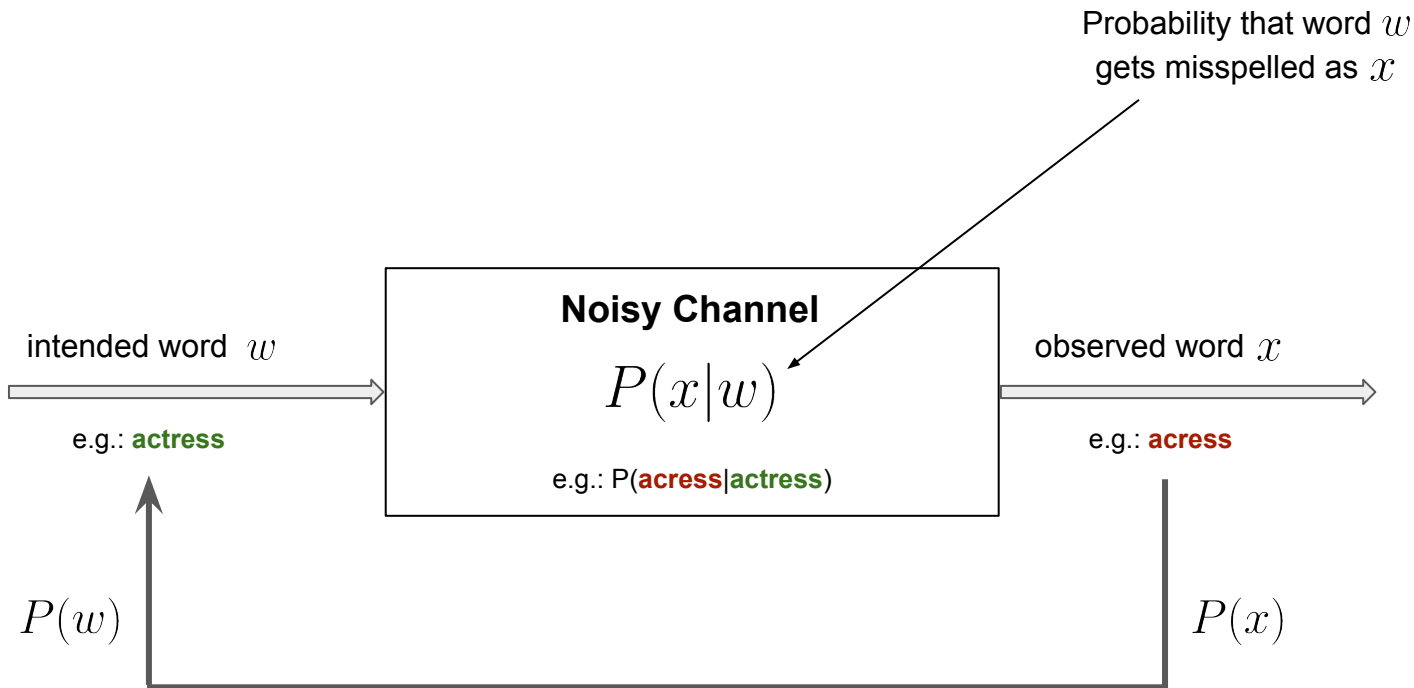
- Ranking of candidates to show top candidates first
- Support for automated spelling correction



## → Noisy Channel Model

Idea: Assign each candidate a probability

# Noisy Channel Model — Intuition



**Decoding:** Observing error  $x$ , can we predict correct word  $w$ ?

# Noisy Channel Model — Bayesian Inferencing

Given an observation  $x$  of a misspelled word,  
find the correct word  $w$ :

$$\hat{w} = \operatorname{argmax}_{w \in V} P(w|x)$$

$$\hat{w} = \operatorname{argmax}_{w \in V} \frac{P(x|w)P(w)}{P(x)}$$

$$\hat{w} = \operatorname{argmax}_{w \in V} P(x|w)P(w)$$

**Quick refresher: Bayes' Theorem**

$$P(A, B) = P(A|B)P(B)$$

$$P(A, B) = P(B|A)P(A)$$

$$\rightarrow P(A|B)P(B) = P(B|A)P(A)$$

$$\rightarrow P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

→ How to calculate  $P(x|w)$  and  $P(w)$  ?

# Noisy Channel Model — Calculating/Estimating $P(w)$

- Approach using Maximum Likelihood Estimate (MLE)

- Required: Large text corpus with  $N$  words
- Calculate/estimate  $P(w)$  with  $P(w) = \frac{freq(w)}{N}$

- Example

- 100 MB Wikipedia dump
- Total of 14.4M+ words

| $w$            | $freq(w)$ | $P(w)$     |
|----------------|-----------|------------|
| <i>actress</i> | 1,135     | 0.0000784  |
| <i>cress</i>   | 1         | 0.00000... |
| <i>caress</i>  | 3         | 0.00000... |
| <i>access</i>  | 1,670     | 0.0001153  |
| <i>across</i>  | 1,756     | 0.0001213  |
| <i>acres</i>   | 177       | 0.0000122  |

**Note:** The frequencies can widely different across different corpora (e.g. Wikipedia articles vs. English Literature).

# Noisy Channel Model — Calculating/Estimating $P(x|w)$

- In general,  $P(x|w)$  almost impossible to predict
  - Predictions depends on arbitrary factors  
(e.g., proficiency of typist, lighting conditions, input device)
- Estimate  $P(x|w)$  based on simplifying assumptions (Kernighan et al., 1990)
  - Most misspelled words in typewritten text are single-error
  - Consider only single-error misspellings: **Insertion**, **Deletion**, **Substitution**, **Transposition**

# Noisy Channel Model — Calculating/Estimating $P(x|w)$

- Definition of 4 confusion matrices (1 for each single-error type)
  - Each confusion matrix lists the number of times one "thing" was confused with another
  - e.g., for substitution, an entry represents the number of times one letter was incorrectly used
- Underlying definitions for generate confusion matrices

|               |                                                        |
|---------------|--------------------------------------------------------|
| $ins[x, y]$   | number of times $x$ was typed as $xy$                  |
| $del[x, y]$   | number of times $xy$ was typed as $x$                  |
| $sub[x, y]$   | number of times $x$ is substituted for $y$             |
| $trans[x, y]$ | number of times $xy$ was typed as $yx$                 |
| $count[x]$    | number of times that $x$ appeared in the training set  |
| $count[x, y]$ | number of times that $xy$ appeared in the training set |

$$x, y \in \{a, b, c, \dots, z\}$$

# Noisy Channel Model — Calculating/Estimating $P(x|w)$

$$P(x|w) = \begin{cases} \frac{ins[w_{i-1}, x_i]}{count[w_i]} & , \text{ if insertion} \\ \frac{del[w_{i-1}, w_i]}{count[w_{i-1}, w_i]} & , \text{ if deletion} \\ \frac{sub[x_i, w_i]}{count[w_i]} & , \text{ if substitution} \\ \frac{trans[w_i, w_{i+1}]}{count[w_i, w_{i+1}]} & , \text{ if transposition} \end{cases}$$

$w_i$  = i-th character in the correct word  $w$

$x_i$  = i-th character in the misspelled word  $x$

# Noisy Channel Model — Calculating/Estimating $P(x|w)$

**sub[X, Y] = Substitution of X (incorrect) for Y (correct)**

| X | Y (correct) |    |    |    |     |   |    |    |     |   |   |    |    |     |    |    |   |    |    |    |    |   |    |   |    |   |
|---|-------------|----|----|----|-----|---|----|----|-----|---|---|----|----|-----|----|----|---|----|----|----|----|---|----|---|----|---|
|   | a           | b  | c  | d  | e   | f | g  | h  | i   | j | k | l  | m  | n   | o  | p  | q | r  | s  | t  | u  | v | w  | x | y  | z |
| a | 0           | 0  | 7  | 1  | 342 | 0 | 0  | 2  | 118 | 0 | 1 | 0  | 0  | 3   | 76 | 0  | 0 | 1  | 35 | 9  | 9  | 0 | 1  | 0 | 5  | 0 |
| b | 0           | 0  | 9  | 9  | 2   | 2 | 3  | 1  | 0   | 0 | 0 | 5  | 11 | 5   | 0  | 10 | 0 | 0  | 2  | 1  | 0  | 0 | 8  | 0 | 0  | 0 |
| c | 6           | 5  | 0  | 16 | 0   | 9 | 5  | 0  | 0   | 0 | 1 | 0  | 7  | 9   | 1  | 10 | 2 | 5  | 39 | 40 | 1  | 3 | 7  | 1 | 1  | 0 |
| d | 1           | 10 | 13 | 0  | 12  | 0 | 5  | 5  | 0   | 0 | 2 | 3  | 7  | 3   | 0  | 1  | 0 | 43 | 30 | 22 | 0  | 0 | 4  | 0 | 2  | 0 |
| e | 388         | 0  | 3  | 11 | 0   | 2 | 2  | 0  | 89  | 0 | 0 | 3  | 0  | 5   | 93 | 0  | 0 | 14 | 12 | 6  | 15 | 0 | 1  | 0 | 18 | 0 |
| f | 0           | 15 | 0  | 3  | 1   | 0 | 5  | 2  | 0   | 0 | 0 | 3  | 4  | 1   | 0  | 0  | 0 | 6  | 4  | 12 | 0  | 0 | 2  | 0 | 0  | 0 |
| g | 4           | 1  | 11 | 11 | 9   | 2 | 0  | 0  | 0   | 1 | 1 | 3  | 0  | 0   | 2  | 1  | 3 | 5  | 13 | 21 | 0  | 0 | 1  | 0 | 3  | 0 |
| h | 1           | 8  | 0  | 3  | 0   | 0 | 0  | 0  | 0   | 0 | 2 | 0  | 12 | 14  | 2  | 3  | 0 | 3  | 1  | 11 | 0  | 0 | 2  | 0 | 0  | 0 |
| i | 103         | 0  | 0  | 0  | 146 | 0 | 1  | 0  | 0   | 0 | 0 | 6  | 0  | 0   | 49 | 0  | 0 | 0  | 2  | 1  | 47 | 0 | 2  | 1 | 15 | 0 |
| j | 0           | 1  | 1  | 9  | 0   | 0 | 1  | 0  | 0   | 0 | 0 | 2  | 1  | 0   | 0  | 0  | 0 | 0  | 5  | 0  | 0  | 0 | 0  | 0 | 0  | 0 |
| k | 1           | 2  | 8  | 4  | 1   | 1 | 2  | 5  | 0   | 0 | 0 | 0  | 5  | 0   | 2  | 0  | 0 | 0  | 6  | 0  | 0  | 0 | 4  | 0 | 0  | 3 |
| l | 2           | 10 | 1  | 4  | 0   | 4 | 5  | 6  | 13  | 0 | 1 | 0  | 0  | 14  | 2  | 5  | 0 | 11 | 10 | 2  | 0  | 0 | 0  | 0 | 0  | 0 |
| m | 1           | 3  | 7  | 8  | 0   | 2 | 0  | 6  | 0   | 0 | 4 | 4  | 0  | 180 | 0  | 6  | 0 | 9  | 15 | 13 | 3  | 2 | 2  | 3 | 0  | 0 |
| n | 2           | 7  | 6  | 5  | 3   | 0 | 1  | 19 | 1   | 0 | 4 | 35 | 78 | 0   | 0  | 7  | 0 | 28 | 5  | 7  | 0  | 0 | 1  | 2 | 0  | 2 |
| o | 91          | 1  | 1  | 3  | 116 | 0 | 0  | 0  | 25  | 0 | 2 | 0  | 0  | 0   | 0  | 14 | 0 | 2  | 4  | 14 | 39 | 0 | 0  | 0 | 18 | 0 |
| p | 0           | 11 | 1  | 2  | 0   | 6 | 5  | 0  | 2   | 9 | 0 | 2  | 7  | 6   | 15 | 0  | 0 | 1  | 3  | 6  | 0  | 4 | 1  | 0 | 0  | 0 |
| q | 0           | 0  | 1  | 0  | 0   | 0 | 27 | 0  | 0   | 0 | 0 | 0  | 0  | 0   | 0  | 0  | 0 | 0  | 0  | 0  | 0  | 0 | 0  | 0 | 0  | 0 |
| r | 0           | 14 | 0  | 30 | 12  | 2 | 2  | 8  | 2   | 0 | 5 | 8  | 4  | 20  | 1  | 14 | 0 | 0  | 12 | 22 | 4  | 0 | 0  | 1 | 0  | 0 |
| s | 11          | 8  | 27 | 33 | 35  | 4 | 0  | 1  | 0   | 1 | 0 | 27 | 0  | 6   | 1  | 7  | 0 | 14 | 0  | 15 | 0  | 0 | 5  | 3 | 20 | 1 |
| t | 3           | 4  | 9  | 42 | 7   | 5 | 19 | 5  | 0   | 1 | 0 | 14 | 9  | 5   | 5  | 6  | 0 | 11 | 37 | 0  | 0  | 2 | 19 | 0 | 7  | 6 |
| u | 20          | 0  | 0  | 0  | 44  | 0 | 0  | 0  | 64  | 0 | 0 | 0  | 0  | 2   | 43 | 0  | 0 | 4  | 0  | 0  | 0  | 0 | 2  | 0 | 8  | 0 |
| v | 0           | 0  | 7  | 0  | 0   | 3 | 0  | 0  | 0   | 0 | 0 | 1  | 0  | 0   | 1  | 0  | 0 | 0  | 8  | 3  | 0  | 0 | 0  | 0 | 0  | 0 |
| w | 2           | 2  | 1  | 0  | 1   | 0 | 0  | 2  | 0   | 0 | 1 | 0  | 0  | 0   | 0  | 7  | 0 | 6  | 3  | 3  | 1  | 0 | 0  | 0 | 0  | 0 |
| x | 0           | 0  | 0  | 2  | 0   | 0 | 0  | 0  | 0   | 0 | 0 | 0  | 0  | 0   | 0  | 0  | 0 | 0  | 9  | 0  | 0  | 0 | 0  | 0 | 0  | 0 |
| y | 0           | 0  | 2  | 0  | 15  | 0 | 1  | 7  | 15  | 0 | 0 | 0  | 2  | 0   | 6  | 1  | 0 | 7  | 36 | 8  | 5  | 0 | 0  | 1 | 0  | 0 |
| z | 0           | 0  | 0  | 7  | 0   | 0 | 0  | 0  | 0   | 0 | 0 | 7  | 5  | 0   | 0  | 0  | 0 | 2  | 21 | 3  | 0  | 0 | 0  | 0 | 3  | 0 |

# Noisy Channel Model — Example

- Noisy channel probabilities for "acress"

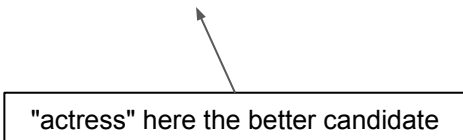
| Candidate Correction | Correct Letter | Error Letter | x w        | P(x w)          | P(w)           | $10^9 \cdot P(x w)P(w)$ | %           |
|----------------------|----------------|--------------|------------|-----------------|----------------|-------------------------|-------------|
| actress              | t              |              | c ct       | .000117         | .0000231       | 2.7                     | 35.9        |
| cress                |                | a            | a #        | .00000144       | .00000054      | .00078                  | ~0          |
| caress               | ca             | ac           | ac ca      | .00000164       | .00000170      | .0028                   | ~0          |
| access               | c              | r            | r c        | .00000021       | .0000916       | .019                    | ~0          |
| <b>across</b>        | <b>o</b>       | <b>e</b>     | <b>e o</b> | <b>.0000093</b> | <b>.000299</b> | <b>2.8</b>              | <b>37.2</b> |
| acres                |                | s            | es e       | .0000321        | .0000318       | 1.0                     | 13.3        |
| acres                |                | s            | ss s       | .0000342        | .0000318       | 1.0                     | 13.3        |

→ Choice of candidate for correction: *across*

# Noisy Channel Model — Discussion

- Basic limitation: No consideration of additional context
  - Model only applicable for non-word errors
  - Basic model will always suggest "across" to correct "acress"

*"The role was played by an **acress** famous for her comedic timing."*



"actress" here the better candidate

→ **Language Models** (next lecture)

# Summary

- RegEx — fundamental and useful tool
- Text Preprocessing — getting your data ready for analysis
  - Tokenization
  - Stemming / Lemmatization
  - Normalization

} **typical very task-dependent!**
- Error Handling (so far)
  - Focus on single-error misspellings
  - Focus on isolated-word error correction

} **already very non-trivial!**

# Outlook for Next Week: Language Models

Image from [Da Nina @ Unsplash](#)

# Pre-Lecture Activity for Next Week

