

CS4248: Natural Language Processing

Lecture 2 — Strings & Words

Outline

Regular Expressions

- **■** Basic Concepts
- Relationship to FSA
- Error Types

Corpus Preprocessing

- Tokenization
- Normalization
- Stemming / Lemmatization
- Segmentation

Word error handling

- Spelling Errors
- Minimum Edit Distance
- Noisy Channel Model

Regular Expressions

- Regular Expression Definition
 - Search pattern used to match character combinations in a string
 - Pattern = sequence of characters

Common applications

- Parse text documents to find specific character patterns
- Validate text to ensure it matches predefined patterns
- Extract, edit, replace, delete substrings matching a pattern

Example: password validation

- * Must have a minimum of 8 characters
- * Must not contain username
- * Must include at least 1 uppercase
- * Must include at least 1 lowercase
- * Must include at least 1 digit or 1 special character: ~!@#\$%^&*_-+=`|\(){}[]:;"'<>,.?/

Two basic search approaches

- Default: match only <u>first</u> occurrence of pattern
- Global search: match <u>all</u> occurrences of pattern (assumed in most following examples)

Basic Patterns

- Fixed patterns
- floor → My block has 15 floors, and I live on floor 5.
 - 5 → My block has 15 floors, and I live on floor 5.
- blocks **→** My block has 15 floors, and I live on floor 5.

Special characters (metacharacters)

Character	Explanation						
	matches any character except line breaks						
^	match the start of a string						
\$	match the end of a string						
ı	matches RegEx either before or after the symbol (e.g., floor floors)						
\b	matches boundary between word and non-word						

Character Classes

- Character class
 - Defines set of valid characters
 - Enclosed using "[...]"
 - Can be negated: "[^...]"
 - [0-9] [0-9] → My block has 15 floors, and I live on floor 5.

 (match all sequences of 2 digits)
 - [. , ; :] → My block has 15 floors, and I live on floor 5.

 (match all sequences of length 1 that are either a period, comma, etc.)
 - [^a-z] \rightarrow My block has 15 floors, and I live on floor 5.

 (match all sequences of length 1 that are not a lowercase letter)

Predefined Character Classes

• Common character classes with their own shorthand notation (i.e., metacharacters)

Class	Alternative	Explanation
\d	[0-9]	matches any digit
\D	[^0-9]	matches any non-digit
\s	[\n\r\t\f]	matches any whitespace character
\s	[^ \n\r\t\f]	matches any non-whitespace character
\w	[a-zA-Z0-9_]	matches any word character
\W	[^a-zA-Z0-9_]	matches any non-word character

Repetition Patterns

- Very common: patterns with flexible lengths, e.g.:
 - All numbers with more than 2 digits
 - All words with less than 5 characters
- Repetition patterns metacharacters

Pattern	Explanation
+	1 or more occurrences
*	0 or more occurrences
3	0 or 1 occurrences
{n}	exactly n occurrences
{1,u}	between 1 and u occurrences; can be unbounded: {1,} or {,u}

Repetition Patterns — Examples

\d{2,} → My block has 15 floors, and I live on floor 5. (match all numbers with 2 or more digits)

\d+ → My block has 15 floors, and I live on floor 5.

(match all numbers with 1 or more digits)

\b\w{2,4}\b \rightarrow My block has 15 floors, and I live on floor 5. (match words with 2 to 4 characters)

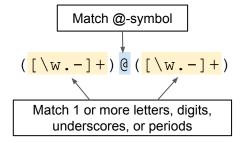
\b[Ff]loor[s]?\b → My block has 15 floors, and I live on floor 5.

(match occurrences of "floor", either capitalized or not, either in singular or plural)

Groups

- Groups: Organizing patterns into parts
 - Groups are enclosed using "(...)"
 - While whole expression must match, groups are captures individually (a match is no longer a string but a tuple of strings, on for each group)
 - Groups can be nested, e.g., (...(...)...((...))...) (order of groups depends on the order in which the groups "open")

Send an email to alice@example.org for more information.



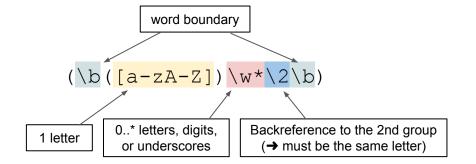
Match:	user@example.org	
Group #1:	alice	
Group #2:	example.org	

Backreferences

- Reference groups within a RegEx
 - Find repeated patterns (see example below)
 - Support only partial replacement of matches

Example:

- "My mom said I need to pass this test."
- Goal: Find all words that start and end with the same letter



Match:	mom	
Group #1:	mom	
Group #2:	m	

Match:	test
Group #1:	test
Group #2:	t

Lookarounds

- Special groups assertions
 - Match like any other group, but do not capture the match
 - 2 types: lookaheads and lookbehinds
 - 2 forms of assertion: positive and negative

	Туре	Example
(?=)	positive lookahead	A (?=B) → finds expr. A but only when followed by expr. B
(?!)	negative lookahead	A (?!B) → finds expr. A but only when not followed by expr. B
(?<=)	positive lookbehind	(?<=B) A → finds expr. A but only when preceded by expr. B
(?)</td <td>negative lookbehind</td> <td>(?<!--B) A → finds expr. A but only when not preceded by expr. B</td--></td>	negative lookbehind	(? B) A → finds expr. A but only when not preceded by expr. B</td

Lookarounds — **Example**

- Positive lookahead
 - "Paying 10 SGD for 1 kg of chicken seems fair."
 - Goal: Extract all *kg* values (numbers followed by the unit *kg*)

$$\d+(?=\s*kg)$$

"Paying 10 SGD for 1 kg of chicken seems fair.

"Paying 10 SGD for 1.5 kg of chicken seems fair.

"Paying 10 SGD for 1,500.00 kg of chicken seems fair.

$$[0-9.,]*[0-9]+(?=\s*kg)$$

"Paying 10 SGD for 1 kg of chicken seems fair.

"Paying 10 SGD for 1.5 kg of chicken seems fair.

"Paying 10 SGD for 1,500.00 kg of chicken seems fair.

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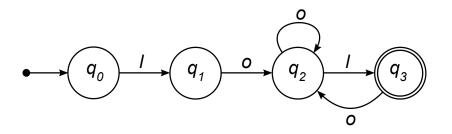
- Spelling Errors
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Relationship to Finite State Automata

Equivalence

- Regular Expressions describe Regular Languages (most restricted types of languages w.r.t Chomsky Hierarchy)
- Regular Language = language accepted by a FSA

Example: FSA that accepts the Regular Language described by the Regular Expression I(o+I)+



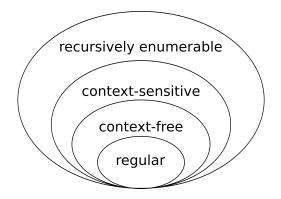
Regular Expression

I(o+I)+

Regular Language {lol, loool, lolol, looolol, ...}

Chomsky Hierarchy

(Source: Wikipedia)



Relationship to Finite State Automata

Basic equivalences

а a ab a | b q_0 a* q_0

In-Lecture Activity (10 mins)



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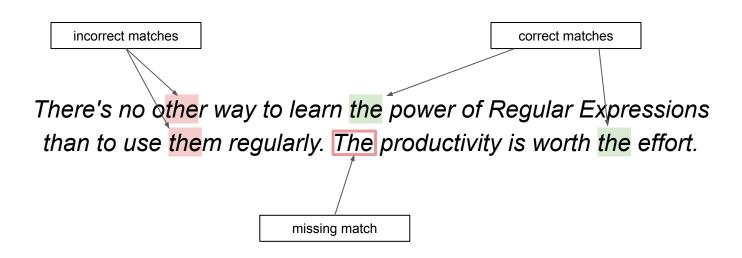
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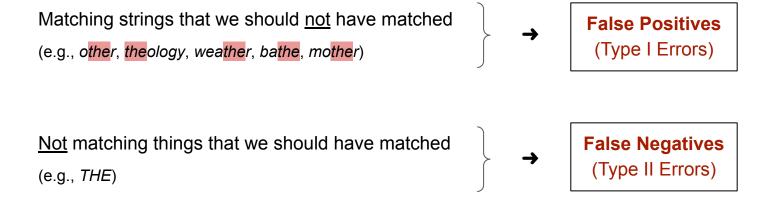
Error Types — What Can Go Wrong

- Example: Find all occurrences of article "the"
 - Naive approach: "the" (fixed pattern)



Error Types

2 basic types of errors



Error Types — Observations

- Many contexts deal with these 2 types of errors, e.g.:
 - Medical testing (e.g., ART test is positive but person is not infected with COVID → false positive)
 - Information retrieval (e.g., a Web search is missing a relevant page → false negative)
 - Document classification (e.g., an abusive tweet has be classified as positive → false positive)
- Reducing errors

false negative false positive

- Both error types not always equally bad (infected person tests negative vs. healthy person test positive)
- Reducing False Positives and False Negatives often in conflict (reducing False Positives often increases False Negatives, and vice versa)

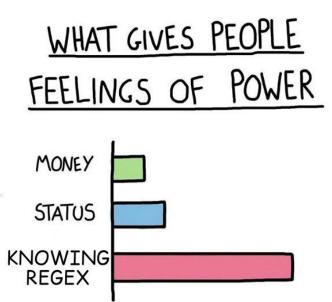
Regular Expressions — Summary

Know their powers

- Extremely useful tool for many
 (low-level) text processing tasks
 (e.g., data preprocessing, tokenization, normalization)
- Important skill for anyone working with strings or text

Know their limitations

- Regular Expressions represent hard rules
- Higher-level text processing task generally require statistical models ("soft" rules)
- → Machine Learning classifiers



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Tokenization

- Tokenization: splitting a string into tokens → vocabulary (set of all unique tokens)
 - Token = character sequence with a semantic meaning (typically: words, numbers, punctuation but may differ depending on applications)
- Very important for step for most NLP algorithms (tokenization errors quickly propagate up → "garbage in, garbage out") Character-based tokenization trivial (e.g., using Regex: .) 3 basic approaches character-S h h е S d r V n g а S t е t а а 0 W е based subword-She 's driv ing fast than allow er ed based word-She 's driving faster than allowed based

Tokenization — Word-Based



- 2 intuitive approaches (solved using RegEx)
 - Match all words, numbers and punctuation marks
- → \w+|\d+|[,.;:]
- Match boundaries between "words" and "non-words" → (?=\W) | (?<=\W)</p>

$$\w+|d+|[,::] \rightarrow NLP$$
 is fun, and there is so much to learn in 13 weeks.

Tokenization — It Quickly Gets Tricky

Multiword phrases → I just came back from New York City.

Common contractions → I'm not home, so don't call.

Hyphenations → NLP is a well-defined but non-trivial topic.

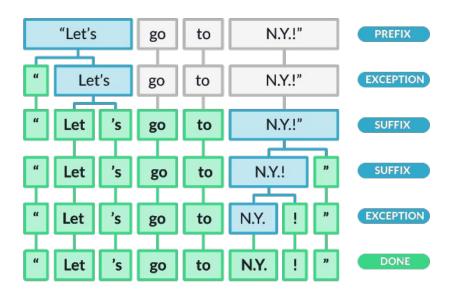
Acronyms, names, etc. → I watched a C++ documentary on T.V.

Special tokens → My email is chris@nus.comp.nus.sg :o)

RegEx used:

\w+|\d+|[,.;:]

Example: spaCy Tokenizer



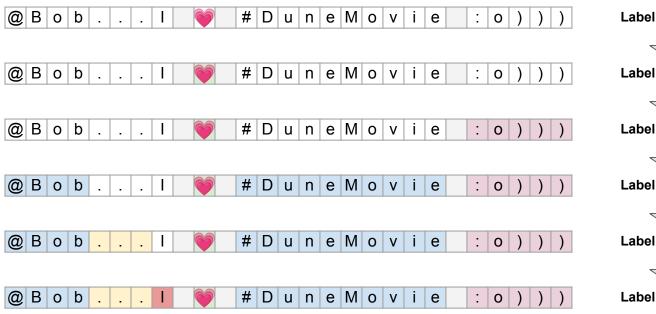
- (1) Split string on whitespace characters
- (2) From left to right, recursively check substrings:
 - Does substring match an exception rule?
 (e.g., "don't" → "do", "n't", but keep "U.K.")
 - Can a prefix, suffix or infix be split of?
 (e.g., commas, periods, quotes, hyphens)

Substring checks based on

- Regular Expressions
- Hand-crafted rules / patterns

Source: https://spacy.io/usage/spacy-101
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Example: Chris's Tokenizer



Sequential labeling of characters

Label all whitespace characters



Label all unicode characters



Label all emoticons



Label all special token types



Label all punctuation marks

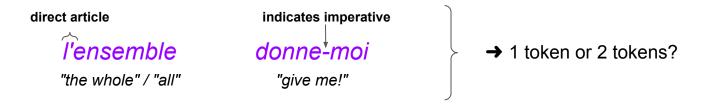


Label all all alphanumeric characters

→ Tokens = Substrings with adjacent characters with the same labels

Tokenization — Language Issues

- French
 - Different uses of apostrophes and hyphens (compared to English)



- German
 - Very common: compound nouns



→ important: compound splitter

Tokenization — Language Issues

dates and amounts

Languages without whitespaces separating words

莎拉波娃 现在 居住 在 美国 东南部 的 佛罗里达 Chinese lives US southeastern Florida Sharapova now フォーチュン500社は情報不足のため時間あた\$500K(約6,000万円) Japanese multiple syllabaries multiple formats for Katakana Romanji Hiragana Kanji

Tokenization — Word Segmentation of Chinese Text

Baseline algorithm: Maximum Matching



莎拉波娃现在居住在美国东南部的佛罗里达



莎拉波娃现在居住在美国东南部的佛罗里达
Sharapova



莎拉波娃现在居住在美国东南部的佛罗里达



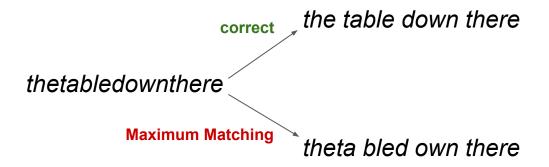
莎拉波娃 **现在**居住在美国东南部的佛罗里达

- (1) Place a pointer at the beginning of the string
- (2) Find longest word in dictionary that matches string starting the pointer
- (3) Mover the pointer over the word in the string
- (4) Goto #2 to process the whole string

Tokenization — Maximum Matching

• Surprisingly good performance on Chinese text (even better performance with probabilistic methods or extensions)

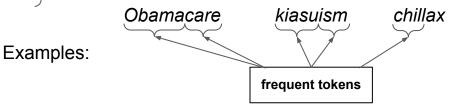
Generally does not work for English text



Tokenization — Subword-Based

- Subword-based tokenization
 - So far: a priori specification of rules (e.g., RegEx) what constitutes valid tokens
 - Now: use data to specify how to tokenize
- Why do we want to do this?
 - Out Of Vocabulary (OOV) words (word/token an NLP model has not seen before)
 - Very rare words in corpus

→ problematic when building statistical models



→ Goal: Split OOV and rare words into (some) known & frequent tokens

Tokenization — Subword-Based

- Different algorithms for subword tokenization
 - <u>Byte-Pair Encoding (BPE)</u>, Unigram Language Model Tokenization, WordPiece, etc.

Different approaches, similar 2-parts setup

(1) Token Learner

Takes raw training corpus and induces a vocabulary (i.e., set of tokens)

(2) Token Segmenter

Takes a raw text and tokenizes it according to vocabulary

Tokenization — BPE Token Learner



Corpus:

"low low low low lower lower newest newest newest newest newest widest widest longer"

special end-of-word token

Initialize vocabulary (e.g., {'d', 'e', 'g', 'i', 'l', 'n', 'o', 'r', 's', 't', 'w', '_')

REPEAT

Find the 2 tokens most frequently adjacent to each other (e.g., 'e', 's')

Add a new merged token 'es' to vocabulary

Replace every adjacent 'e' 's' in corpus with 'es'

UNTIL k merges have been done

Tokenization — BPE Token Learner

corpus representation

6	n	е	W	е	S	t	_
5	1	0	W	_			
3	W	i	d	е	s	t	_
2	1	0	W	е	r	_	
1	1	0	n	g	е	r	_

vocabulary

merges



most frequent pair: e & s (9 occurrences)

corpus representation

6	newest_
5	1 o w _
3	widest_
2	lower_
1	longer_

vocabulary

merges

(e, s)



most frequent pair: es & t (9 occurrences)

Tokenization — BPE Token Learner

corpus representation

6	n	е	W	est _	
5	1	0	W	_	
3	W	i	d	est _	
2	1	0	W	er_	
1	1	0	n	ger	_

vocabulary

d, e, g, i, l, n, o, r, s, t, w, _, es, est

merges



most frequent pair: est & _ (9 occurrences)

corpus representation

6	n	е	W	est_
5	1	0	W	_
3	W	i	d	est_
2	1	0	W	er_
1	1	0	n	ger_

vocabulary

merges



most frequent pair: 1 & o (8 occurrences)

Tokenization — BPE Token Learner

corpus representation

6	n e w est_
5	lo w _
3	w i d est_
2	lower_
1	longer_

vocabulary

d, e, g, i, l, n, o, r, s, t, w, _, es, est, est_, lo

merges



most frequent pair: 10 & w (7 occurrences)

corpus representation

6	n e w est_
5	low _
3	w i d est_
2	low e r _
1	longer_

vocabulary

merges



most frequent pair: n & e (6 occurrences)

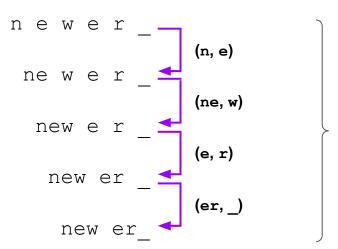
Tokenization — BPE Token Learner

```
d, e, g, i, l, n, o, r, s, t, w, _, es, est, est , lo, low, ne
   merges (e, s), (es, t), (est, ), (1, 0), (10, w), (n, e)
vocabulary d, e, g, i, l, n, o, r, s, t, w, _, es, est, est , lo, low, ne, new
   merges (e, s), (es, t), (est, ), (1, o), (1o, w), (n, e), (ne, w)
vocabulary
            d, e, g, i, l, n, o, r, s, t, w, _, es, est, est , lo, low, ne, new, newest
   merges (e, s), (es, t), (est, ), (1, o), (1o, w), (n, e), (ne, w), (new, est)
```

Tokenization — BPE Token Segmenter

Tokenize/segment "newer"

Run each merge in order they have been learned



→ tokens: "new", "er_"

Tokenization — Summary

- Tokenization as low-level NLP task
 - Challenges: important, non-trivial, language-dependent
 - Particularly tricky for informal language (e.g., social media)
- 3 basic approaches
 - Character-based (trivial to do but often not suitable individual characters generally carry no semantic meaning)
 - Word-based (a priori specification of rules; language-dependent; problem: OOV/rare words)
 - Subword-based (tokenization learned from data tokens are often morphemes!)
- Practical consideration (when using off-the-shell word-based tokenizers)
 - What is my type of text (e.g., formal or informal)? Are there special tokens (e.g., URLs, hashtags)?
 - Try and assess different tokenizers very, very last resort: write your own tokenizer

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Normalization

- Goal: Convert text into a canonical (standard) form
 - Remove noise / "randomness" from text
 - Affects characters, <u>words</u>, sentences, documents
- Implicit definition of equivalence classes
 - Suitable normalization steps depend on task/application

Alternative to equivalence classes: asymmetric expansion

Example: Web Search (utilize case of search terms)

Entered term

window

window

windows

Windows

Windows

Windows

Windows

Windows

Raw	Normalized
Germany GERMANY	germany
USA U.S.A US of A	USA
tonight tonite 2N8	tonight
connects connected connecting connection	connect
:) :-) :o)	smile

Normalization — Case Folding

When to fold?

- Common application: Information Retrieval (e.g., Web search where must users type only in lowercase anyway)
- Potential problems: *Bush* vs. *bush*, *MOM* vs. *mom*, *Cloud* vs. *cloud*, etc. (potential exception: upper case word in mid sentence?)

When NOT to fold?

- NLP tasks where case of letters or words are important features
- Examples: Named Entity Recognition, Machine Translation

They sent us a card from the US during their vacation.

Distinction important for NER and MT!

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Normalization — Stemming & Lemmatization

Motivating example:

"dogs make the best friends" vs. "a dog makes a good friend"

→ Very similar semantics but (very) different syntax

- Common reasons for variations of the same word
 - Singular vs. plural form (mainly of nouns)
 - Different tenses of verbs
 - Comparative/superlative of adjectives

→ Can we normalize words to abstract from such variations?

Normalization — Stemming

Idea of Stemming

- Reduce words to their stem.
- Approach: crude chopping of affixes based on rules (→ language dependent)
- Different stemmers apply different rules

Characteristics

- Pro: fast + no lexicon required
- Con: stemmed word not necessarily a proper word (i.e., not in dictionary)

Examples

(alternatives reflect results from different stemmers)

Raw	Stemmed
cats	cat
running	run
phones	phon(e)
presumably	presum
crying	cry/cri
went	went
worse	wors
best	best
mice	mic(e)

Normalization — Stemming: Porter Stemmer

- Porter Stemmer most common stemmer for English text
 - Simple, efficient + very good results in practice
- Series of rewrite rules that run in a cascade
 - Output of each pass is fed is input to the next pass
 - Stemming steps if a pass yields no more changes

	sses → ss	e.g.: possesses → possess, classes → class
	tional → tion	e.g., optional → option, fictional → function
	ies → i	e.g., <i>cries</i> → <i>cri</i> , <i>tries</i> → <i>tri</i>
stem must contain vowel ——	- (*v*)ing → ε	e.g.: $sing \rightarrow sing$, $singing \rightarrow sing$, $talking \rightarrow talk$
stem must contain >1 chars ——	-(m>1)ement → ε	e.g., replacement → replac, cement → cement

Normalization — Lemmatization

- Idea of Lemmatization
 - Reduce inflections or variant forms to base form
 - Find the correct dictionary headword form
 - Differentiates between word forms: nouns (N), verbs (V), adjectives (A)

Raw	Lemmatized (N)	Lemmatized (V)	Lemmatized (A)
running	running	run	running
phones	phone	phone	phones
went	went	go	went
worse	worse	worse	bad
mice	mouse	mice	mice

Normalization — Lemmatization: Characteristics

Pros

- Lemmatized words are proper words (i.e., dictionary words)
- Can normalize irregular forms (e.g., $went \rightarrow go, worst \rightarrow bad$)

Cons

- Requires curated lexicons / lookup tables + rules (typically)
- Requires Part-of-Speech tags for correct results
- Generally slower as stemming

Normalization — Stemming & Lemmatization

Back to our motivating example

Raw: "dogs make the best friends" "a dog makes a good friend"

Stemmed: "dog make the best friend" "a dog make a good friend"

Lemmatized: "dog make the good friend" "a dog make a good friend"

Normalization — Final Words

- Canonical form also effects tokenization, e.g.: Penn Treebank Tokenizer
 - Separate out clitics (e.g., doesn't → does n't; John's → John 's)
 - Keep hyphenated words together
 - Separate out all punctuation symbols
- Other common normalization steps
 - Removal of stopwords (e.g., a, an, the, not, and, or, but, to, from, at)
 - Removal of non-standard tokens (e.g., URs, emojis, emoticons)
 - **...**

Quick Quiz



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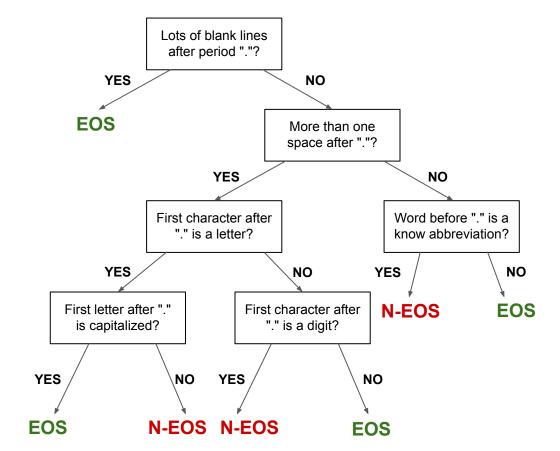
Sentence Segmentation

- Sound like a simple task but...
 - Period "." can be quite ambiguous (e.g., "1.25", "U.S.A.", "Dr.") "?", "!" relatively unambiguous
 - Poor punctuation in informal text (common: missing whitespaces, missing capitalization)
 - → RegEx for segmenting sentences quickly become very complex

```
Example RegEx: (?<!\w\.\w.) (?<![A-Z][a-z]\.) (?<=\.|\?)\s (Source: Stackoverflow)
```

- Alternative: binary classifier
 - Consider each period "." in a text
 - Classify: EndOfSentence or NotEndOfSentence
 - → Possible approaches: handwritten rules, set of RegEx, machine learning

Example: Simple Rules (represented as a binary Decision Tree)





Many Other Features Conceivable

- Example: numerical features
 - length of word before / after period "."
 - Distance (in #chars) to next punctuation mark
 - Probabilities derived from a dataset (e.g., probability of with "." occurs at the end of sentence)

Side note: In informal text (e.g., social media) people often use emoticons or emojis to separate sentences, making this task even more complicated.

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Spelling Errors

Non-word error detections

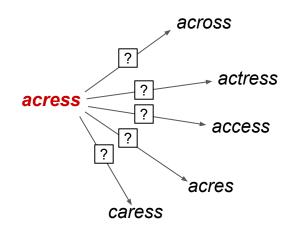
- Basically, word is not found in dictionary
- Example: detecting *graffe* (misspelling of giraffe)

2. Isolated-word error correction

- Consider word in isolation (i.e., without surrounding words)
- Example: correcting *graffe* to *giraffe*

3. Context-sensitive error detection & correction

- Consider surrounding words to detect and correct errors
- Important for "wrong" words that a spelled correctly
- Examples: there vs. three, dessert vs. desert, son vs. song



Spelling Errors — Common Patterns

Observation

- Most misspelled words in typewritten text are single-error
- Damerau (1964): 80%, Peterson (1986): 93-95%

Single-error misspellings

- Insertion (e.g., acress vs. acres)
- Deletion (e.g., *acress* vs. *ac<u>t</u>ress*)
- Substitution (e.g., acress vs. acress)
- Transposition (e.g., <u>acress</u> vs. <u>caress</u>)

For <u>non-word</u> errors:

- → Good candidates are orthographically similar
- → Minimum Edit Distance

Outline

Regular Expressions

- Basic Concepts
- Relationship to FSA
- Error Types

Corpus Preprocessing

- Tokenization
- Normalization
- Stemming / Lemmatization
- Segmentation

Word error handling

- Spelling Errors
- Minimum Edit Distance
- Noisy Channel Model

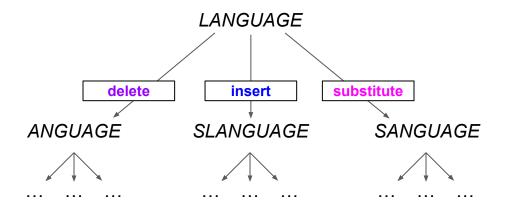
Minimum Edit Distance (MED)

- Minimum Edit Distance between 2 strings s₁ and s₂
 - Minimum number of allowed edit operations to transform s_1 into s_2
 - Allowed edit operations: Insertion, Deletion, Substitution, Transposition ← Not covered here to keep examples simple
- Example
 - s₁ = "LANGUAGE"
 - $s_2 = "SAUSAGE"$

MED if all operations cost 1 → 4

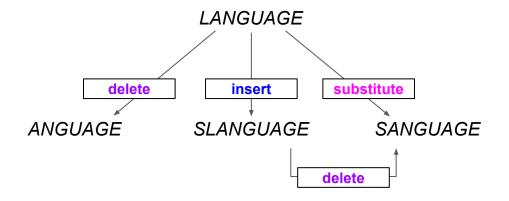
MED if Substitution costs 2, Insertion 1, Deletion 1 → 5

- Problem formulation: Find a path (i.e., sequence of edits) from start string to final string
 - Initial state: the word being transformed (e.g., "LANGUAGE")
 - Target state: the word being transformed into (e.g., "SAUSAGE")
 - Operators: insert, delete, substitute
 - Path cost: aggregated costs of all edits



- → Potentially huge search space
- → Naive navigation of all path impractical

- Observations
 - Many distinct paths end up in the same state



- → No need to keep track of all paths
- → Only important: "cheapest" path to each revisited state (best in terms of costs, not just number of operations!)
- → Solve using **Dynamic Programming**solving problems by combining solutions to subproblems

- Input: 2 strings
 - lacksquare Source string X of length n
 - lacktriangle Target string Y of length m



• Define D(i,j) as MED between $X[\dot{0}..i]$ and $Y[\dot{0}..j]$

ightharpoonup MED between X and Y is thus D(n,m)

- Bottom-up approach of Dynamic Programming
 - Compute D(i, j) for small i, j (base cases)
 - Compute D(i,j) for larger i, j based on previously computes D(i,j) for smaller i, j

Initialization of bases cases

- lacksquare D(i,0)=i (getting from X[0..i] to empty target string requires i deletions)
- lacksquare D(0,j)=j (getting from empty source string to Y[0..j] requires j insertions)
- For $0 < i \le n$ and $0 < j \le m$

$$D(i,j) = min \begin{cases} D(i-1,j) + 1 & \text{Delete} \\ D(i,j-1) + 1 & \text{Insert} \\ D(i-1,j-1) + \begin{cases} 2, & if X[i] \neq Y[j] \\ 0, & if X[i] = Y[j] \end{cases}$$
 Substitute

Assumptions for costs

Insert:

Delete:

Substitute: 2

→ Levenshtein MED

Complexity analysis

Space: O(nm)

Time: O(nm)

Minimum Edit Distance — Calculation Example

\mathbf{E}	8	3			$\int D$	(i-1,j)) + 1 De	lete		
\mathbf{G}	7			$D(i,j) = min \begin{cases} D(i-1,j) + 1 & \text{Delete} \\ D(i,j-1) + 1 & \text{Insert} \\ D(i-1,j-1) + \begin{cases} 2, & if X[i] \neq Y[i] \\ 0, & if X[i] = Y[i] \end{cases} \\ \text{Substitute} \end{cases}$						
\mathbf{A}	6									
\mathbf{U}	5									
\mathbf{G}	4									
N	3									
\mathbf{A}	2									
\mathbf{L}	1									
#	0	1	2	3	4	5	6	7		
	#	S	A	U	S	A	\mathbf{G}	\mathbf{E}		

Minimum Edit Distance — Calculation Example

\mathbf{E}	8	9	8	7	8	7	6	5
\mathbf{G}	7	8	7	6	7	6	5	6
A	6	7	6	5	6	5	6	7
\mathbf{U}	5	6	5	4	5	6	7	8
\mathbf{G}	4	5	4	5	6	7	6	7
N	3	4	3	4	5	6	7	8
A	2	3	2	3	4	5	6	7
L	1	2	3	4	5	6	7	8
#	0	1	2	3	4	5	6	7
	#	S	\mathbf{A}	U	S	A	G	${f E}$

Minimum Edit Distance — Backtrace & Alignments

- Current limitation
 - Base algorithms only returns the MED
 - Often important: alignment between strings

L A N G U * A G E
| | | | | | | | | | | |
S A * * U S A G E

How do we get this?

- Keep track of backtrace
 - Remember from which "direction" we entered a new cell

Keep set of pointers for each $i,\,j$

 At the end, trace path from upper right corner to read of alignment Small extension to base algorithm:

$$PTR(i,j) = \begin{cases} \text{LEFT} & \text{Insert} \\ \text{DOWN} & \text{Delete} \\ \text{DIAG} & \text{Substitute} \end{cases}$$

Note: Backtraces are generally not unique → different alignments for the same MED possible

Minimum Edit Distance — Backtrace & Alignments

\mathbf{E}	8	$\swarrow \leftarrow \downarrow 9$	↓ 8	↓ 7	∠ ←↓ 8	↓ 7	↓ 6	✓ 5
\mathbf{G}	7	∠ ← ↓ 8	↓ 7	↓ 6	$\swarrow \leftarrow \downarrow 7$	↓ 6	✓ 5	← 6
A	6	$\swarrow \leftarrow \downarrow 7$	$\swarrow\downarrow 6$	↓ 5	$\swarrow \leftarrow \downarrow 6$	✓ 5	← 6	← 7
\mathbf{U}	5	$\swarrow \leftarrow \downarrow 6$	1 5	∠ 4	$\leftarrow 5$	← 6	←↓ 7	∠ ←↓ 8
\mathbf{G}	4	$\swarrow \leftarrow \downarrow 5$	$\downarrow 4$	$\swarrow \leftarrow \downarrow 5$	$\swarrow \leftarrow \downarrow 6$	$\swarrow \leftarrow \downarrow 7$	✓ 6	← 7
N	3	$\swarrow \leftarrow \downarrow 4$	↓ 3	$\checkmark\leftarrow\downarrow 4$	$\swarrow \leftarrow \downarrow 5$	$\swarrow \leftarrow \downarrow 6$	$\swarrow \leftarrow \downarrow 7$	∠ ← ↓ 8
A	2	$\swarrow \leftarrow \downarrow 3$	$\swarrow 2$	← 3	← 4	$\checkmark \leftarrow 5$	← 6	← 7
\mathbf{L}	1	$\checkmark\leftarrow\downarrow 2$	$\swarrow \leftarrow \downarrow 3$	$\checkmark\leftarrow\downarrow 4$	$\checkmark\leftarrow\downarrow 5$	$\swarrow \leftarrow \downarrow 6$	$\swarrow \leftarrow \downarrow 7$	∠ ←↓ 8
#	0	1	2	3	4	5	6	7
	#/	S	\mathbf{A}	U	S	A	\mathbf{G}	\mathbf{E}





Complexity analysis

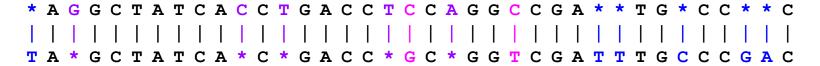
Time: O(n+m)

Minimum Edit Distance — More Examples

Biology: Align 2 sequences of nucleotides

AGGCTATCACCTGACCTCCAGGCCGATGCCC
TAGCTATCACGACCGCGGTCGATTTGCCCGAC

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		$5 \mid \checkmark \downarrow 14 \mid \checkmark \downarrow 13 \mid \checkmark 12 \mid \leftarrow 13 \mid$	$\leftarrow 14$ $\checkmark \leftarrow 15$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	4 / IE 14		V 3
	# ₹ ←2 10 2 14	4 $/\downarrow 13$ $/ 12$ $/\leftarrow 13$ $\leftarrow 14$	← 15
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	3 / 14 13	3 / 12 / 13 / 14 + 15	< 16 ∠< 17
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	2	2 ← 13 ← 14 ← 15 ✓ ← 16 ←	←↓ 17
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1 / 12 - 13	$3 \leftarrow 14 \leftarrow 15 \leftarrow 16 \leftarrow 17$	116 / ← 117
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	2 ← 13 ← 14	$4 \leftarrow 15 \leftarrow \downarrow 16 / \leftarrow \downarrow 17 \downarrow 16$	√ 15 ← 16
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	3 ← 14 / ← 15	5 ←↓16 ↓15 ∠←↓16 ∠15	← 16 ← 17
C 24 23 22 21 \(\sqrt{20} \) 19 \(\psi 18 \) \(\sqrt{19} \) \(\psi 18 \) \(\sqrt{11} \) \(\psi 18 \) \(\psi 17 \) \(\psi 16 \) \(\psi 15 \) \(\psi 18 \) \(\psi 17 \) \(\psi 18 \) \	4 ∠←↓15 ∠←↓16	6 / 15 / 1	18
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		5 / 14 /←	17
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	4 / 15 / 14	4 ∠ (15 Z (1 MED =	15
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			15
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		4 ←↓15 /←↓1	. 18
C 19 118 117 116 215 114 2 15	3 /←↓14 /←↓15	5 / 14 /←	17
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		4 /←15 /←16 / 15 ← 16	← 17
T 17 / 16 15 14 13 / 12 + 13 / 12 + 13 / 12 + 13 / 12 + 11 10 19 5 17 16 15 / + 16 / + 17 / + 18 / + 19 / 8 + 9 + 10 + 11 / + 12 / + 1	3 /← 14 ← 15	5 ←↓16 ↓15 /←↓16 /←↓17 /←	← ↓ 18 _/ ← ↓ 19
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	4 /← 15 /←1 16		← 17
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	3 /←↓14 /←↓15	5 / 14 / ← 15 / ← 16 ← 17	← 18 /← 19
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2 ← 13 ← 14		← 19 ← 20
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	3 ← 14 /← 15		← 20 ← 21
T 12 /111 110 /+111 110 /19 18 /7 16 15 14 /+15 /+16 15 /+16 /+17 /+18 /+19 /+110 /9 +10 +11 +12 /+13 /+1			← 21 ← 22
C 11 \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \			< 22 / ← ↓ 23
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			⊢↓ 23
			√ 22 ← 23
$\begin{bmatrix} \mathbf{c} & \mathbf{s} & 17 \end{bmatrix}$ $\begin{bmatrix} 16 & 2 \leftarrow 17 \end{bmatrix}$ $\begin{bmatrix} 16 & 2 \leftarrow 18 \end{bmatrix}$ $\begin{bmatrix} 16 $	8 /←↓19 /←1 20		← 23 /← 24
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			← 24 ← 25
A = 6 + 15 + 24 + 15 + 14 + 13 + 22 + 3 + 24 + 25 + 25 + 25 + 25 + 25 + 25 + 25			← 25 ← 26
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			← 26 ← 27
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			← 27 \/ ← 28
G 3 /-14 13 /12 /-13 /-14 /-15 /-16 /-17 /-18 /-19 /8 -9 -10 -11 /-12 -13 /-14 /-15 -16 -17 /-18 -19 -20 -2			← 28 ← 29
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			← 29 ← 30
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			← 30 ← 31
# 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 2			31 32
# T A G C T A T C A C G A C C G C G G T C G A T	T T G	3 C C C G	Λ C
		2 0 0 0	



In-Lecture Activity (10 mins)



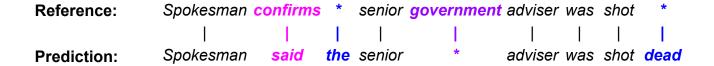
In-Lecture Activity (10 mins)



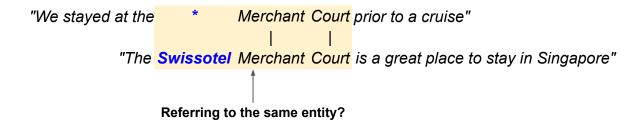
Minimum Edit Distance — Other Uses in NLP

Evaluating Machine Translation and speech recognition

e.g., How similar are 2 translations?



Named Entity Extraction and Entity Coreference



Minimum Edit Distance — Extensions

- Weighted Minimum Edit Distance, e.g.:
 - Spell Correction: some letters are more likely to be mistyped than others
 - Biology: certain kinds of deletions or insertions are more likely than others

→ Generalization of algorithm

Application-dependent weights (i.e., costs for edit operations)

Initialization of base cases:

$$\begin{split} &D(0,0) = 0 \\ &D(i,0) = D(i-1,0) + del(X[i]), & \text{for } 1 < i \le n \\ &D(0,j) = D(0,j-1) + ins(Y[i]), & \text{for } 1 < i \le m \end{split}$$

Recurrence relation:

$$D(0,0) = 0$$

$$D(i,0) = D(i-1,0) + del(X[i]), \text{ for } 1 < i \le n$$

$$D(i,j) = min\begin{cases} D(i-1,j) & + del(X[i]) \\ D(i,j-1) & + ins(Y[j]) \\ D(i-1,j-1) & + sub(X[i],Y[i]) \end{cases}$$

Minimum Edit Distance — Extensions

- Needleman-Wunsch
 - No penalty for gaps (*) at the beginning or the end of an alignment
 - Good if strings have very different lengths
- Smith-Wasserman
 - Ignore badly aligned regions
 - Find optimal <u>local</u> alignments within substrings (Levenshtein finds the best global distance and alignment)

Common application:
Alignment of nucleotides sequences

Outline

Regular Expressions

- Basic Concepts
- Relationship to FSA
- Error Types

Corpus Preprocessing

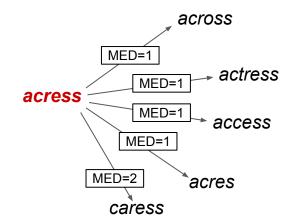
- Tokenization
- Normalization
- Stemming / Lemmatization
- Segmentation

Word error handling

- Spelling Errors
- Minimum Edit Distance
- Noisy Channel Model

Where We are Right Now

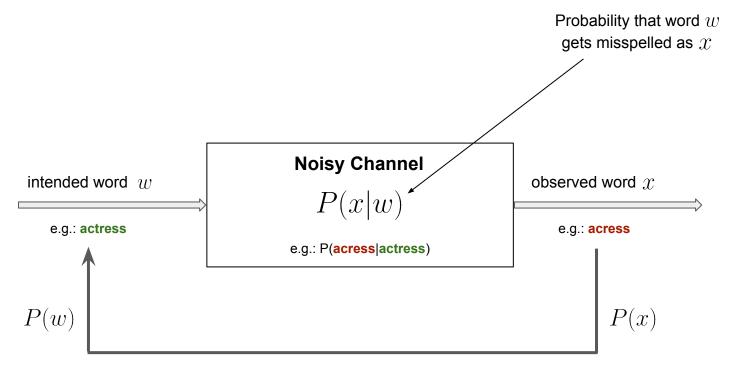
- Given a misspelled word, generate suitable candidates for error correction
 - 80% of errors are within minimum edit distance 1
 - Almost all errors within minimum edit distance 2
 - Covers also missing spaces and hyphens (e.g., thisidea vs. this idea; inlaw vs. in-law)
- Still missing: Which is the most likely candidate?
 - Ranking of candidates to show top candidates first
 - Support for automated spelling correction



→ Noisy Channel Model

Idea: Assign each candidate a probability

Noisy Channel Model — **Intuition**



Decoding: Observing error x, can we predict correct word w?

Noisy Channel Model — Bayesian Inferencing

Given an observation x of a misspelled word, find the correct word w:

$$\widehat{w} = \underset{w \in V}{\operatorname{argmax}} P(w|x)$$

$$\widehat{w} = \underset{w \in V}{\operatorname{argmax}} \frac{P(x|w)P(w)}{P(x)}$$

$$\widehat{w} = \underset{w \in V}{\operatorname{argmax}} P(x|w)P(w)$$

P(A,B) = P(A|B)P(B)

$$P(A, B) = P(A|B)P(B)$$
$$P(A, B) = P(B|A)P(A)$$

Quick refresher: Bayes' Theorem

→
$$P(A|B)P(B) = P(B|A)P(A)$$

→ $P(A|B) = \frac{P(B|A)P(A)}{P(B)}$

 \rightarrow How to calculate P(x|w) and P(w)?

- Approach using Maximum Likelihood Estimate (MLE)
 - $\ \blacksquare \$ Required: Large text corpus with N words
 - $\qquad \text{Calculate/estimate } P(w) \quad \text{with} \quad P(w) = \frac{freq(w)}{N}$

Example

- 100 MB Wikipedia dump
- Total of 14.4M+ words

w	freq(w)	P(w)				
actress	1,135	0.0000784				
cress	1	0.00000				
caress	3	0.00000				
access	1,670	0.0001153				
across	1,756	0.0001213				
acres	177	0.0000122				

Note: The frequencies can widely different across different corpora (e.g. Wikipedia articles vs. English Literature).

- In general, P(x|w) almost impossible to predict
 - Predictions depends on arbitrary factors (e.g., proficiency of typist, lighting conditions, input device)
- ullet Estimate P(x|w) based on simplifying assumptions (Kernighan et al., 1990)
 - Most misspelled words in typewritten text are single-error
 - Consider only single-error misspellings: Insertion, Deletion, Substitution, Transposition

- Definition of 4 confusion matrices (1 for each single-error type)
 - Each confusion matrix lists the number of times one "thing" was confused with another
 - e.g., for substitution, an entry represents the number of times one letter was incorrectly used

Underlying definitions for generate confusion matrices

ins[x,y]	number of times x was typed as xy
del[x,y]	number of times xy was typed as $\ x$
sub[x,y]	number of times x is substituted for y
trans[x,y]	number of times xy was typed as yx
count[x]	number of times that \boldsymbol{x} appeared in the training set
count[x,y]	number of times that xy appeared in the training set

$$x, y \in \{a, b, c, ..., z\}$$

$$P(x|w) = \begin{cases} \frac{ins[w_{i-1}, x_i]}{count[w_i]} &, \text{ if insertion} \\ \frac{del[w_{i-1}, w_i]}{count[w_{i-1}, w_i]} &, \text{ if deletion} \\ \frac{sub[x_i, w_i]}{count[w_i]} &, \text{ if substitution} \\ \frac{trans[w_i, w_{i+1}]}{count[w_i, w_{i+1}]} &, \text{ if transposition} \end{cases}$$

 $w_i\,$ = i-th character in the correct word $\,w\,$

 x_i = i-th character in the misspelled word x

X	İ					sub	[X, Y	Y] =	Sub	stit	utio			(inc		ct) f	or '	Y (c	orre	ect)						
Λ	a	b	c	d	e	f	o	h	i	i	k	1	m	n	0	n	а	r	S	t	u	V	w	X	V	Z
0	0	0	7	1	342	0	g 0		118	0	1	0	0	3	76	0 0	q 0	1	35	9	9	0	1	0	<u>y</u> 5	0
a b	0	0	9	9	2	2	3	1	0	0	0	5	11	5	0	10	0	0	2	1	0	0	8	0	0	0
2000	6	5	0	16	0	9	5	0	0	0	1	0	7	9	1	10	2	5	39	40	1	3	7	1	1	0
c d	1	10	13	0	12	0	5	5	0	0	2	3	7	3	0	1	0	43	30	22	0	0	4	0	2	0
e	388	0	3	11	0	2	2	0	89	0	0	3	0	5	93	0	0	14	12	6	15	0	1	0	18	0
f	0	15	0	3	1	0	5	2	0	0	0	3	4	1	0	0	0	6	4	12	0	0	2	0	0	0
o	4	1	11	11	9	2	0	0	0	1	1	3	0	0	2	1	3	5	13	21	0	0	1	0	3	0
g h	1	8	0	3	0	0	0	0	0	0	2	0	12	14	2	3	0	3	1	11	0	0	2	0	0	0
i	103	0	0	0		0	1	0	0	0	0	6	0	0	49	0	0	0	2	1	47	0	2	1	15	0
i	0	1	1	9	0	0	1	0	0	0	0	2	1	0	0	0	0	0	5	0	0	0	0	0	0	0
k	1	2	8	4	1	1	2	5	0	0	0	0	5	0	2	0	0	0	6	0	0	0	4	0	0	3
1	2	10	1	4	0	4	5	6	13	0	1	0	0	14	2	5	0	11	10	2	0	0	0	0	0	0
m	1	3	7	8	0	2	0	6	0	0	4	4	0	180	0	6	0	0	9	15	13	3	2	2	3	0
n	2	7	6	5	3	0	1	19	1	0	4	35	78	0	0	7	0	28	5	7	0	0	1	2	0	2
0	91	1	1	3	116	0	0	0	25	0	2	0	0	0	0	14	0	2	4	14	39	0	0	0	18	0
p	0	11	1	2	0	6	5	0	2	9	0	2	7	6	15	0	0	1	3	6	0	4	1	0	0	0
q	0	0	1	0	0	0	27	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
r	0	14	0	30	12	2	2	8	2	0	5	8	4	20	1	14	0	0	12	22	4	0	0	1	0	0
S	11	8	27	33	35	4	0	1	0	1	0	27	0	6	1	7	0	14	0	15	0	0	5	3	20	1
t	3	4	9	42	7	5	19	5	0	1	0	14	9	5	5	6	0	11	37	0	0	2	19	0	7	6
u	20	0	0	0	44	0	0	0	64	0	0	0	0	2	43	0	0	4	0	0	0	0	2	0	8	0
V	0	0	7	0	0	3	0	0	0	0	0	1	0	0	1	0	0	0	8	3	0	0	0	0	0	0
W	2	2	1	0	1	0	0	2	0	0	1	0	0	0	0	7	0	6	3	3	1	0	0	0	0	0
X	0	0	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9	0	0	0	0	0	0	0
y	0	0	2	0	15	0	1	7	15	0	0	0	2	0	6	1	0	7	36	8	5	0	0	1	0	0
Z	0	0	0	7	0	0	0	0	0	0	0	7	5	0	0	0	0	2	21	3	0	0	0	0	3	0

Noisy Channel Model — **Example**

Noisy channel probabilities for "acress"

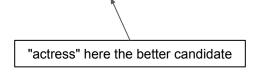
Candidate Correction	Correct Letter	Error Letter	x w	P(x w)	P(w)	10 ⁹ *P(x w)P(w)	%
actress	t		c ct	.000117	.0000231	2.7	35.9
cress		а	a #	.00000144	.00000054	.00078	~0
caress	ca	ac	ac ca	.00000164	.00000170	.0028	~0
access	С	r	r c	.00000021	.0000916	.019	~0
across	O	е	e o	.0000093	.000299	2.8	37.2
acres		S	es e	.0000321	.0000318	1.0	13.3
acres		S	ss s	.0000342	.0000318	1.0	13.3

→ Choice of candidate for correction: across

Noisy Channel Model — Discussion

- Basic limitation: No consideration of additional context
 - Model only applicable for non-word errors
 - Basic model will always suggest "across" to correct "acress"

"The role was played by an acress famous for her comedic timing."



→ Language Models (next lecture)

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- Segmentation

Word error handling

- Spelling Errors
- Minimum Edit Distance
- Noisy Channel Model

Summary

- RegEx fundamental and useful tool
- Text Preprocessing getting your data ready for analysis
 - Tokenization
 - Stemming / Lemmatization
 - Normalization

typical very task-dependent!

- Error Handling (so far)
 - Focus on single-error misspellings
 - Focus on isolated-word error correction

already very non-trivial!

Pre-Lecture Activity for Next Week



Solutions to Quick Quizzes



Solutions to Quick Quizzes

